

A Theoretical Framework for Symbolic Quick Error Detection

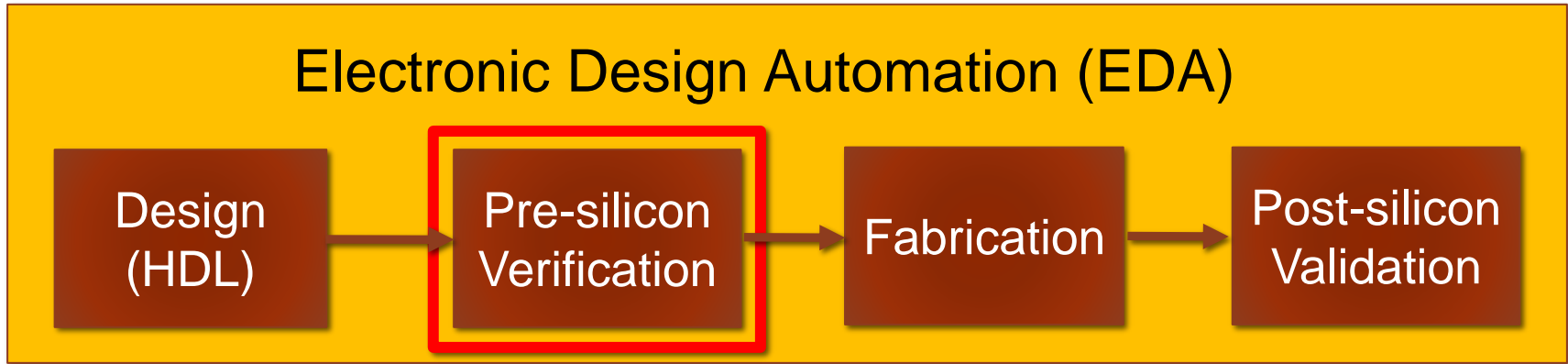


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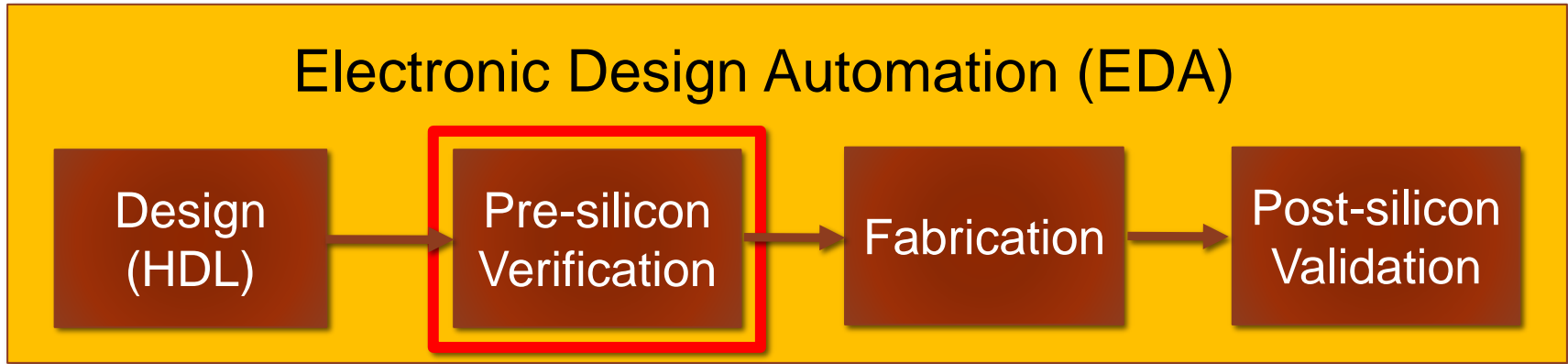
Preprint: <https://arxiv.org/abs/2006.05449>

Context: Pre-Silicon Verification



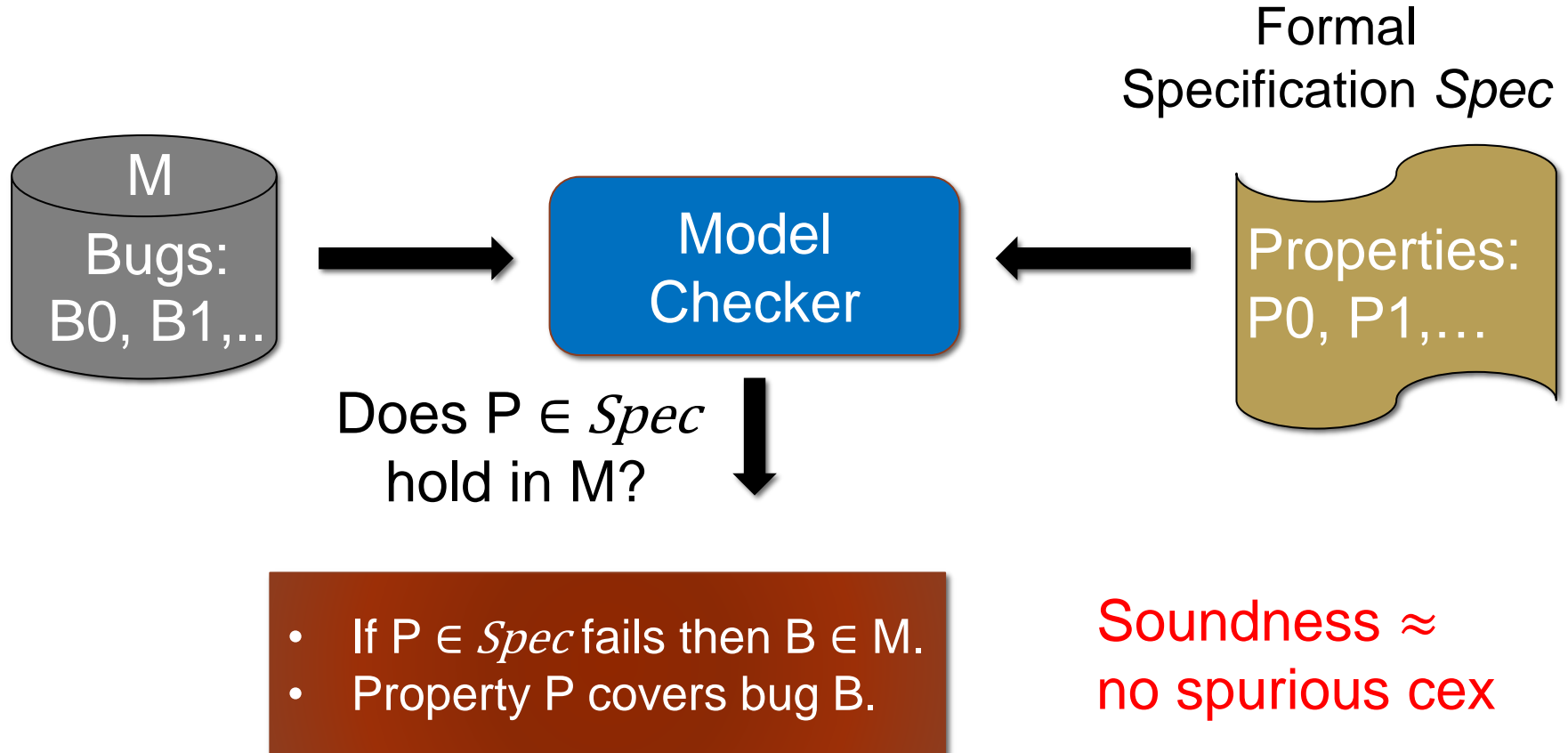
- Our focus: processor designs.
- Formally verify model of a design (e.g. Verilog).
- Model checking vs. non-formal simulation or testing.

Context: Pre-Silicon Verification

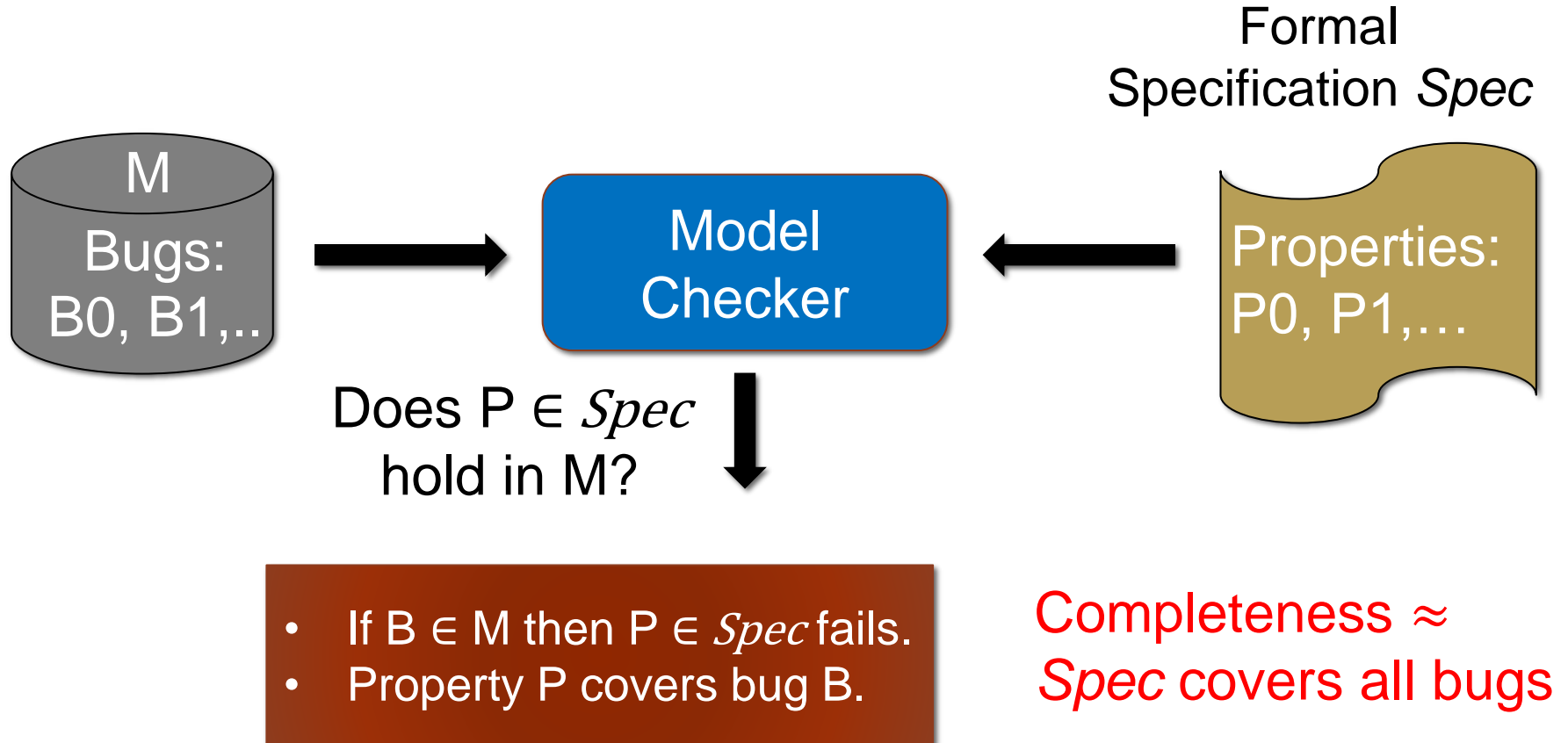


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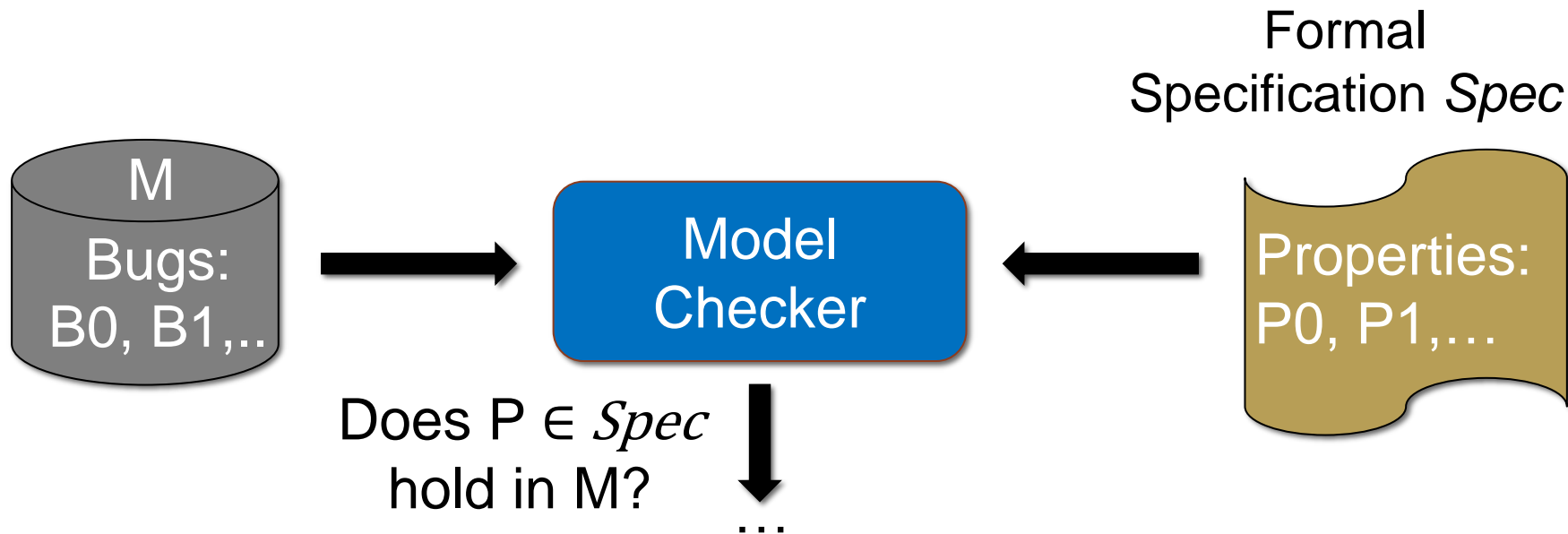
Soundness of Bug-Finding



Completeness of Bug-Finding

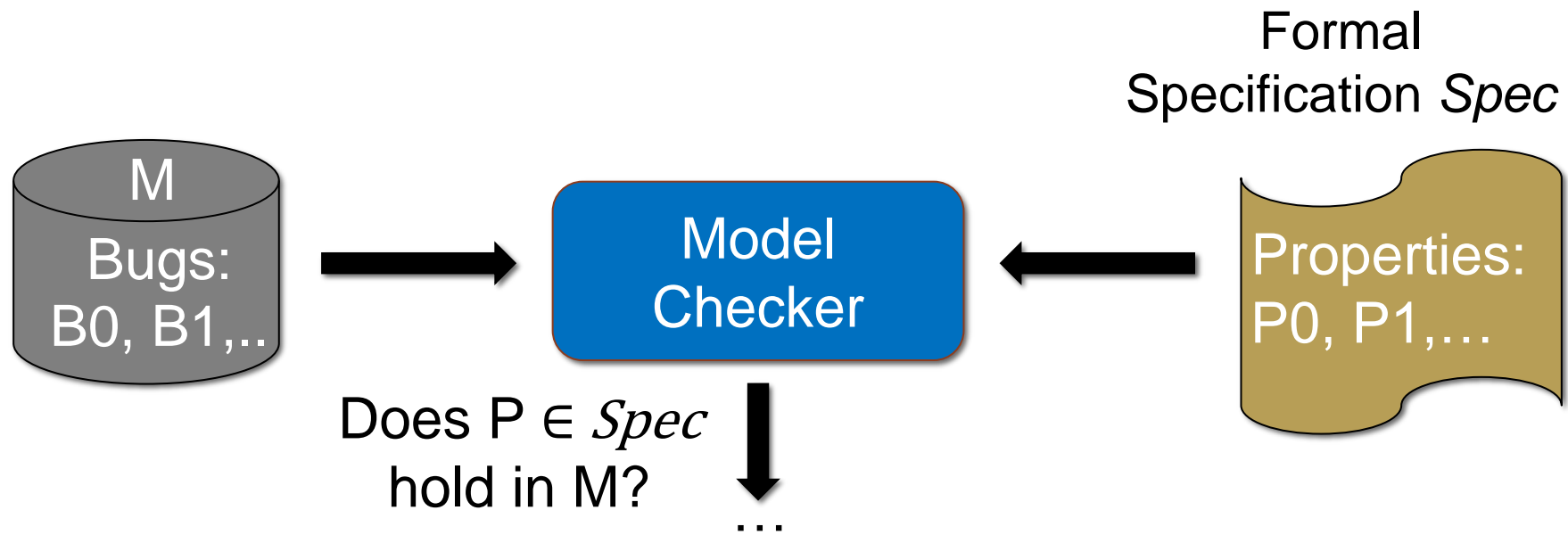


Completeness of Bug-Finding



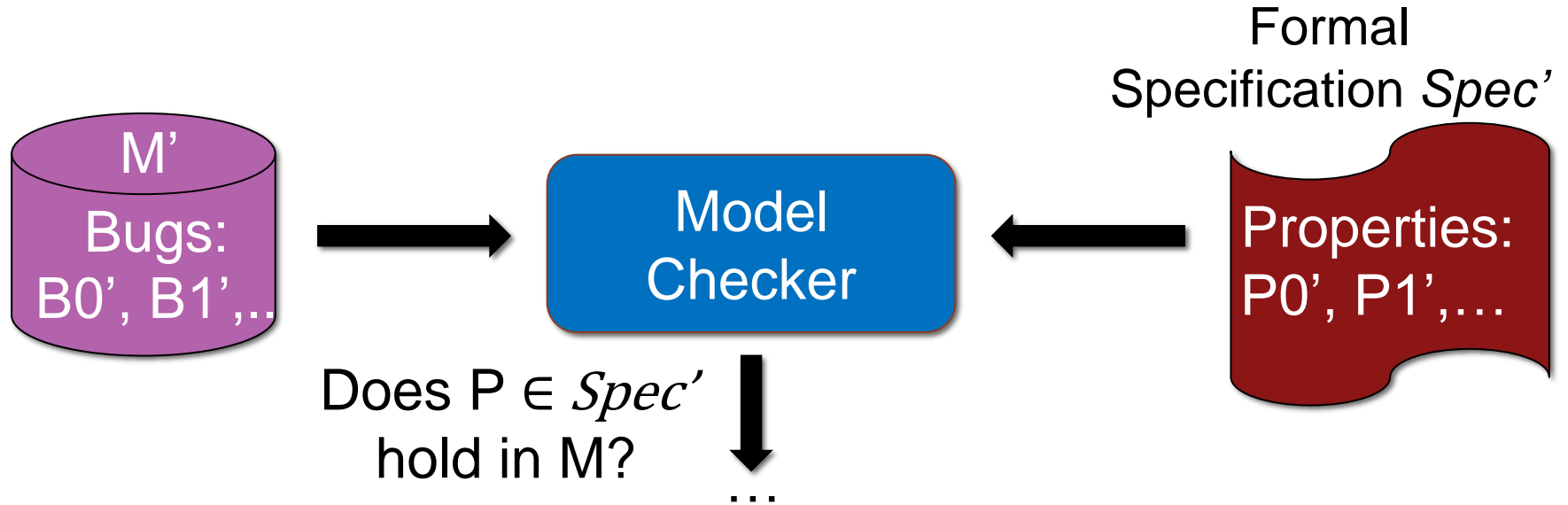
- “Have I written enough properties?” [Katz et al. CHARME’99].
- **Challenge:** making $Spec$ complete.

Challenge: Completeness of Bug-Finding



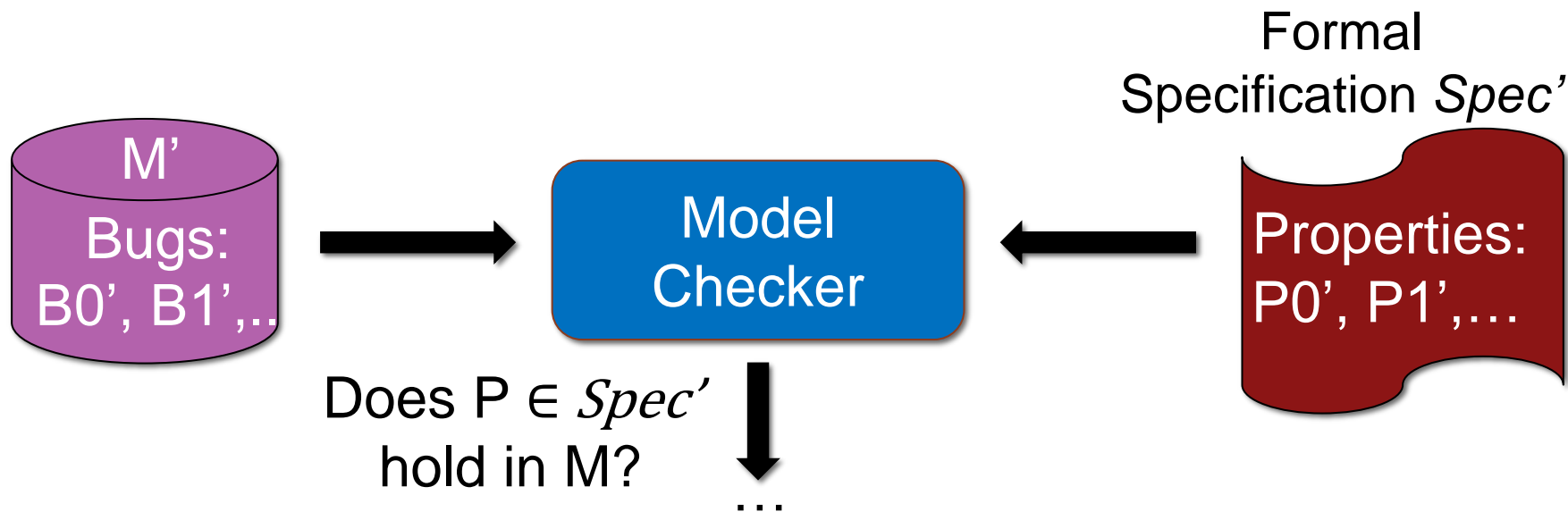
- *Spec*: manual writing of implementation-specific properties.

Challenge: Completeness of Bug-Finding



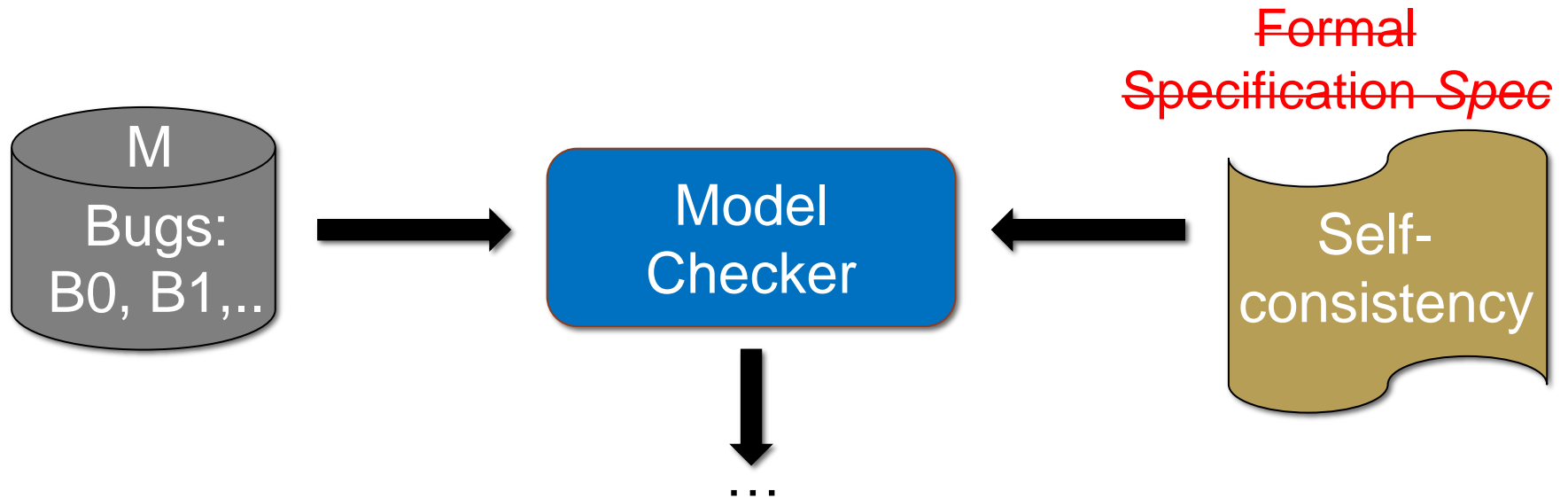
- $Spec$: manual writing of implementation-specific properties.
- Model/design changes \rightarrow $Spec$ to be adapted (manually).

Challenge: Completeness of Bug-Finding



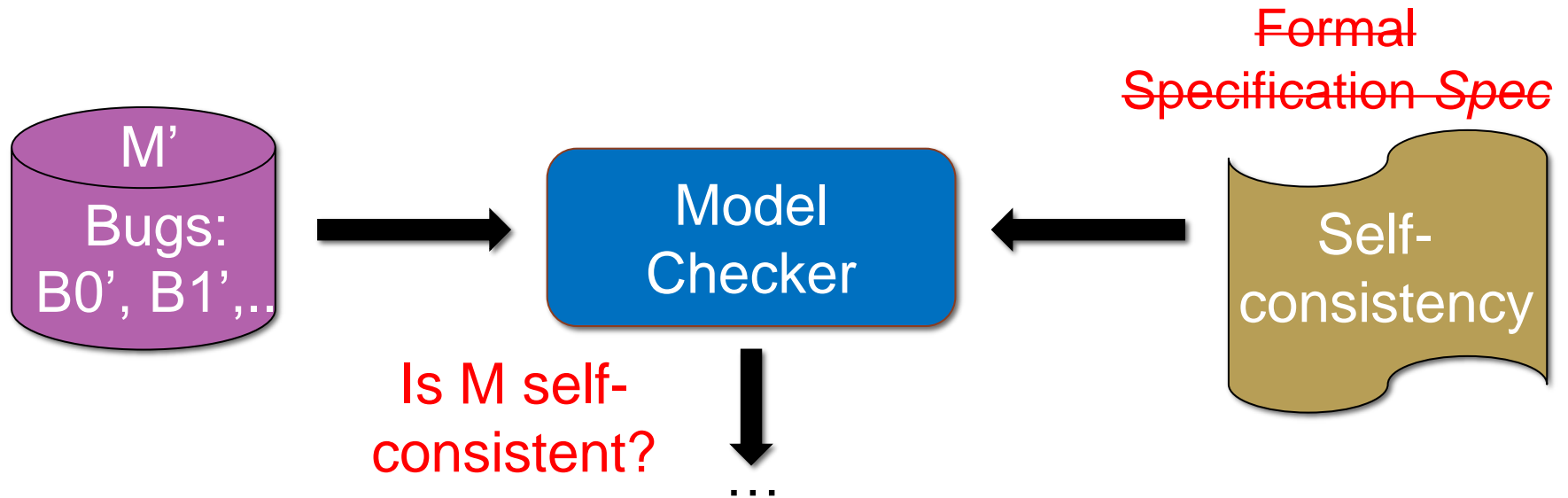
- $Spec$: manual writing of implementation-specific properties.
- Model/design changes \rightarrow $Spec$ to be adapted (manually).
- Completeness depending on $Spec$.

Symbolic Quick Error Detection (SQED)



- **No** need for *Spec* or implementation-specific properties.
- Leverages bounded model checking (BMC).

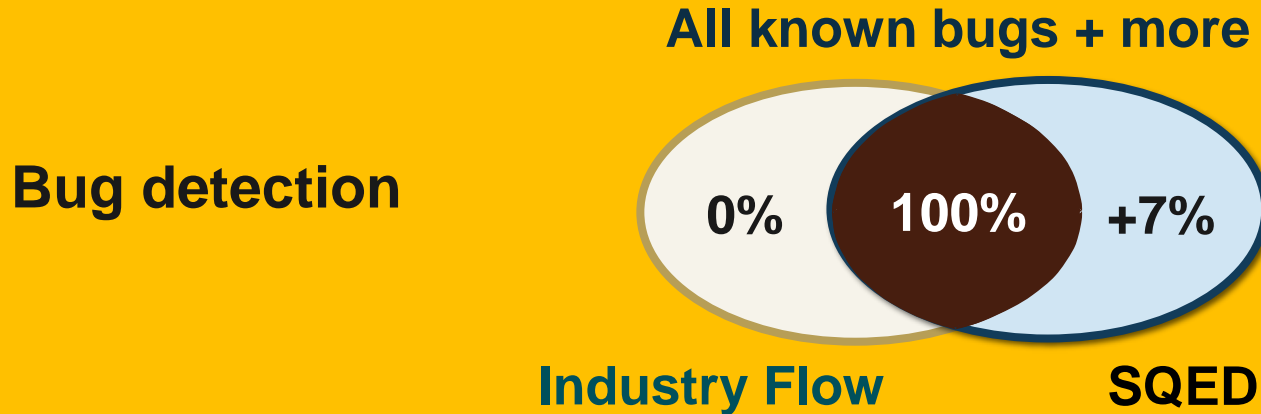
Symbolic Quick Error Detection (SQED)



- **No** need for *Spec* or implementation-specific properties.
- Leverages bounded model checking (BMC).
- **Self-consistency**: universal property, **no** manual writing.

SQED: Industrial Strength

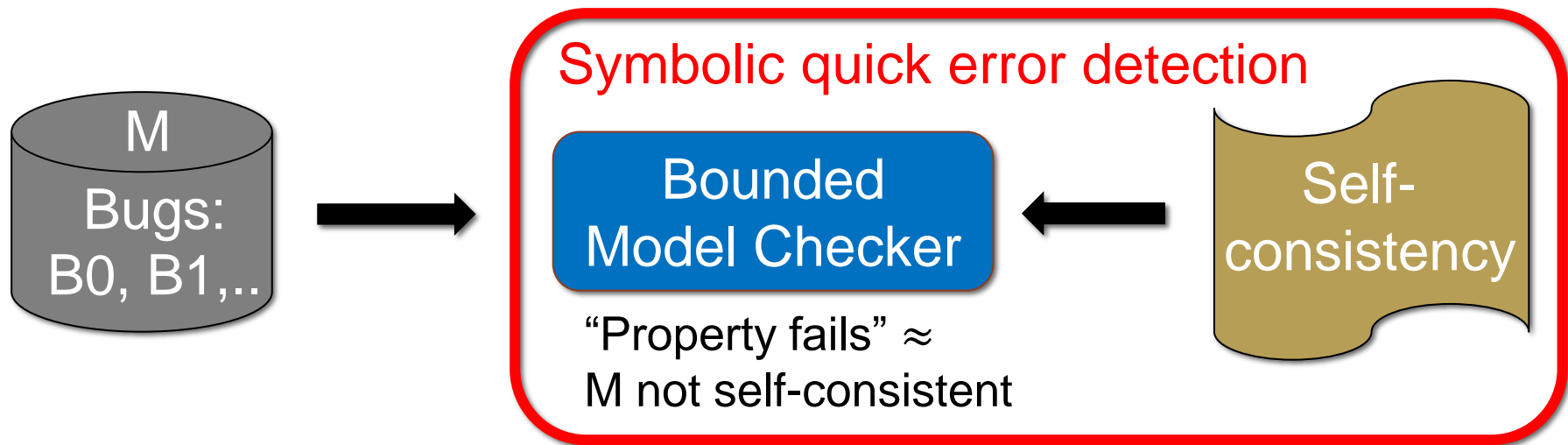
INFINEON case study: automotive IP versions [Singh et al DATE'19]



Traditional verification:

(Constrained) random simulation, directed tests, formal.

Our Contributions: Formal Proofs



1. Soundness: no spurious cex.
2. (Conditional) completeness: all bugs covered (BMC depth).
3. Formal framework: abstract processor model.

Self-Consistency

- Function f : equivalent inputs \rightarrow equivalent outputs.
- Functional congruence property:

$$\forall x, x' : x = x' \rightarrow f(x) = f(x')$$

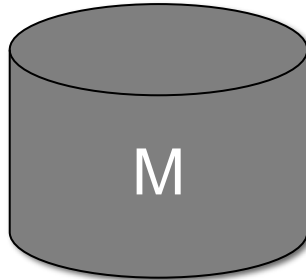
Self-Consistency

- Processor Design M:

$i_1, i_2, \dots, i_n +$
inputs (regs/mem)

=

$i_1', i_2', \dots, i_n' +$
inputs' (regs/mem)



outputs (regs/mem)

=

outputs' (regs/mem)

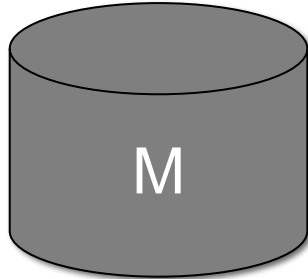
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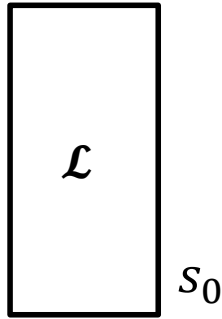


outputs' (regs/mem)



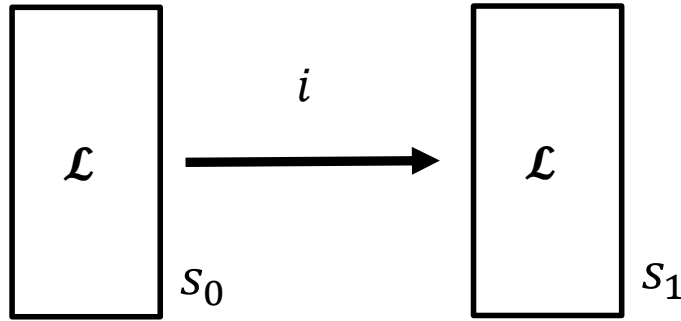
HW designs have complex internal state (pipeline,...).

Formal Model of Processors and SQED



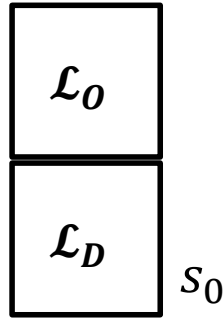
- State s_0 : mapping from locations \mathcal{L} to values.
- (Non-)architectural parts of $s_0 = (s_a, s_{na})$.
- \mathcal{L} : regs. and mem. locations, value $s_0(l) = s_a(l) = v$.

Formal Model of Processors and SQED



- Instruction $i = (op, l, (l', l''))$, one-step execution.
- Opcode op , input locations (l', l'') , output location l .
- Transition: $T(s_0, i) = s_1$, $s_0 = (s_a, s_{na})$, $s_1 = (s_a', s_{na}')$.

Formal Model of Processors and SQED



Example: register identifiers

$$\mathcal{L} = \{0, 1, \dots, 31\}$$

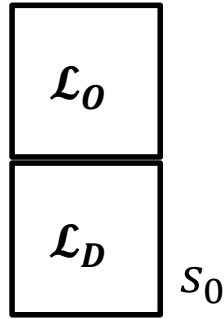
$$\mathcal{L}_O = \{0, \dots, 15\}$$

$$\mathcal{L}_D = \{16, \dots, 31\}$$

$$L_D(l) = l + 16$$

- Partition of \mathcal{L} : original and duplicate locations $\mathcal{L}_O, \mathcal{L}_D$.
- Arbitrary, fixed bijective mapping $L_D : \mathcal{L}_O \rightarrow \mathcal{L}_D$.
- **Self-consistency property** based on mapping L_D .

Formal Model of Processors and SQED



Example:

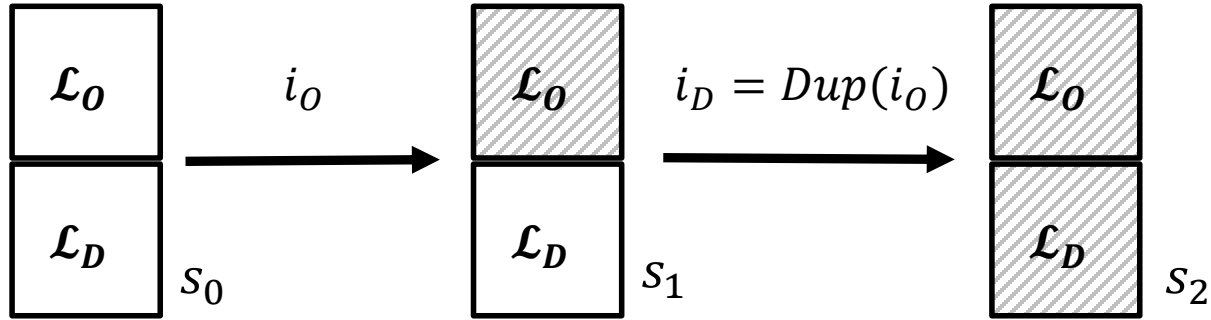
$$i_O = (\text{ADD}, l_{12}, (l_4, l_8))$$

$$L_D(l) = l + 16$$

$$i_D = (\text{ADD}, l_{28}, (l_{20}, l_{24}))$$

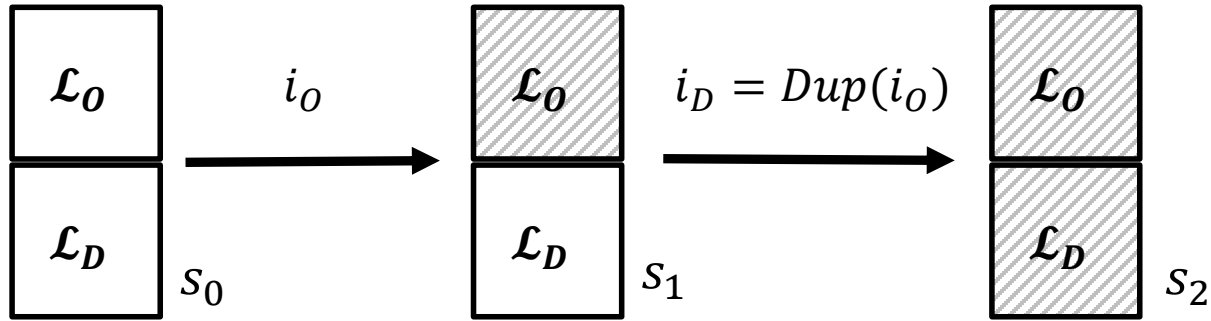
- Original instruction $i_O = (op, l, (l', l''))$.
- Duplicate $i_D = Dup(i_O) = (op, L_D(l), L_D(l', l''))$.

Formal Model of Processors and SQED



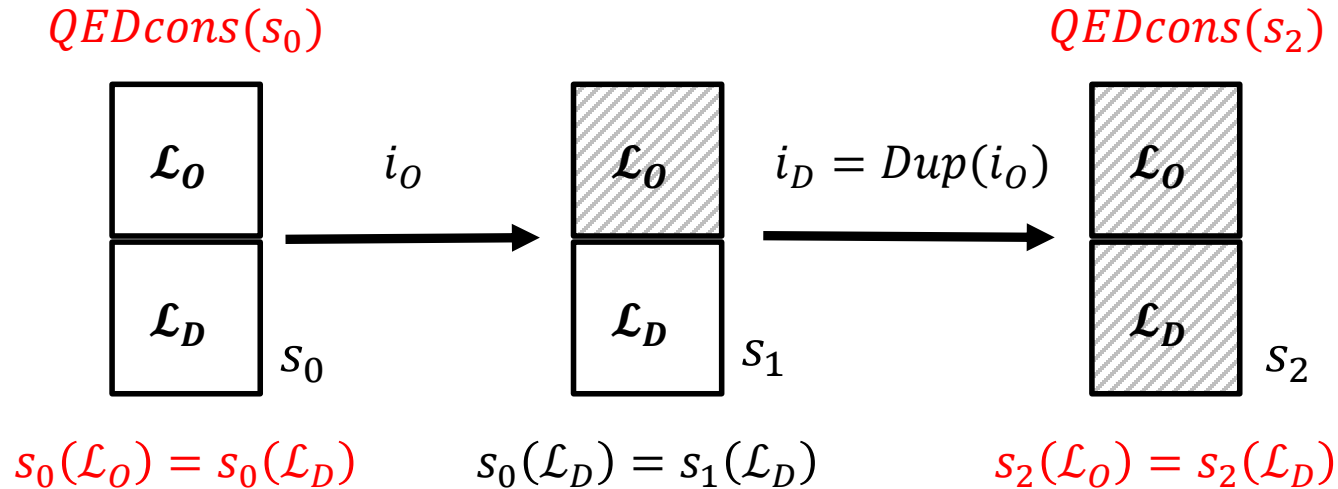
- Original instruction $i_O = (op, l, (l', l''))$.
- Duplicate $i_D = Dup(i_O) = (op, L_D(l), L_D(l', l''))$.
- Original/duplicate i_O/i_D operates on $\mathcal{L}_O/\mathcal{L}_D$ only.

Formal Model of Processors and SQED



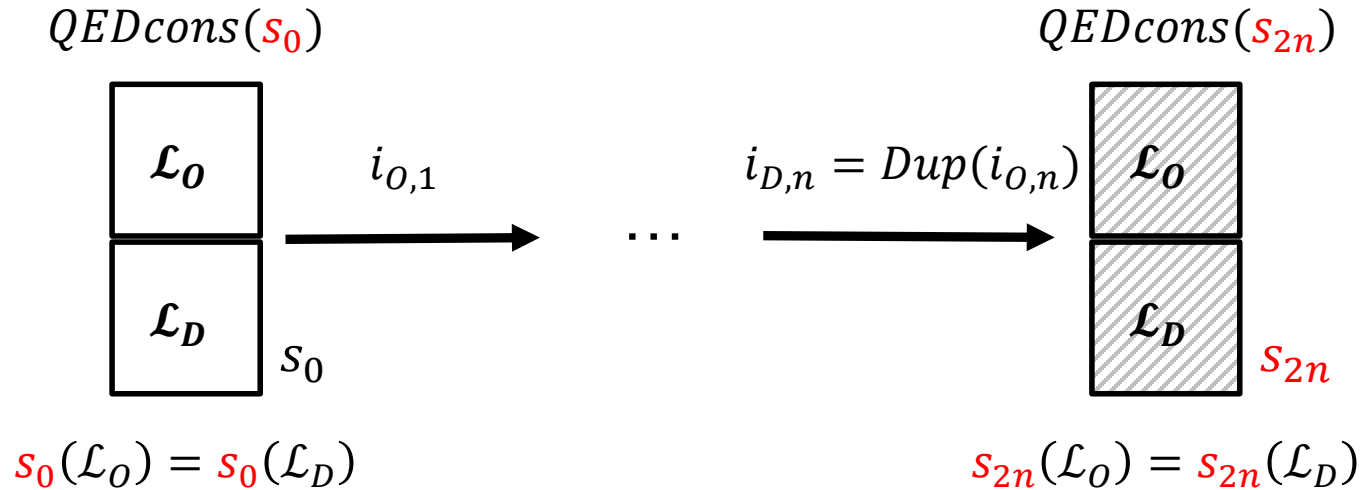
- Given \mathcal{L}_D , state s_0 **QED-consistent** $\leftrightarrow s_0(\mathcal{L}_O) = s_0(\mathcal{L}_D)$.
- Matching values at original/duplicate locations.

Formal Model of Processors and SQED



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- Matching values at original/duplicate locations.
- **Correct** execution of i_0/i_D preserves QED-consistency.

Formal Model of Processors and SQED



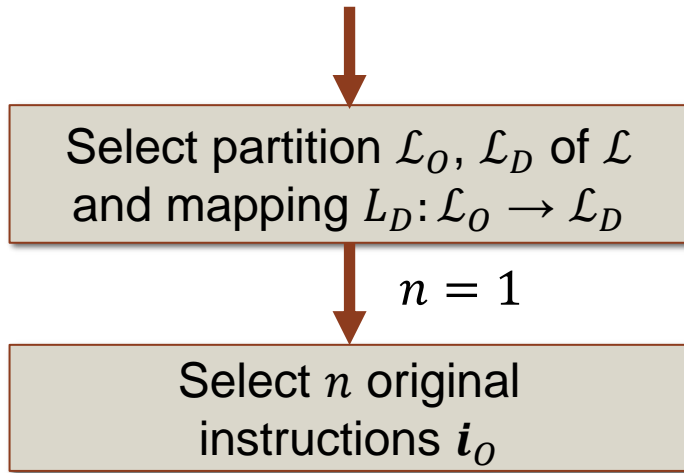
- $\mathbf{i}_O = i_{O,1}, \dots, i_{O,n}$ and $\mathbf{i}_D = i_{D,1}, \dots, i_{D,n}$ with $\mathbf{i}_D = Dup(\mathbf{i}_O)$.
- **QED test:** concatenation $\mathbf{i} = \mathbf{i}_O :: \mathbf{i}_D$ of $2n$ instructions.
- **Correct** execution of \mathbf{i} preserves QED-consistency.

Using BMC in SQED

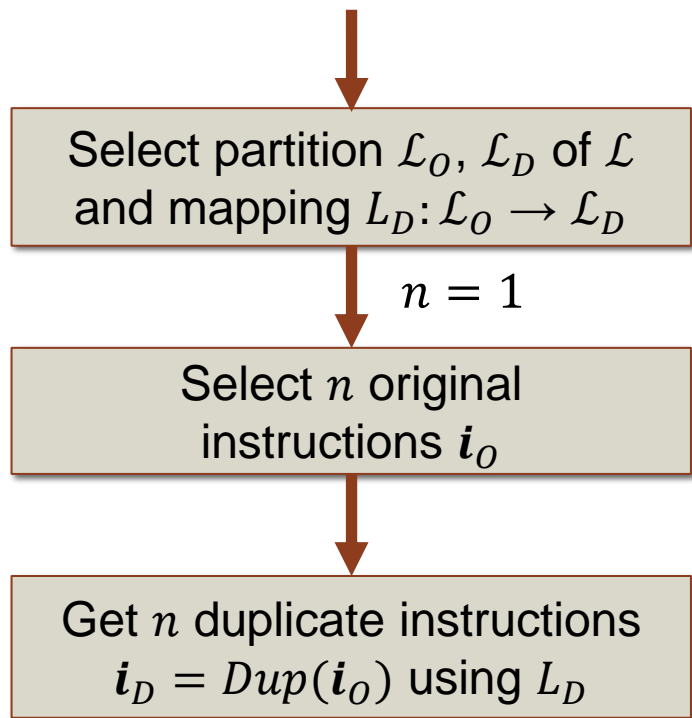


Select partition $\mathcal{L}_O, \mathcal{L}_D$ of \mathcal{L}
and mapping $L_D: \mathcal{L}_O \rightarrow \mathcal{L}_D$

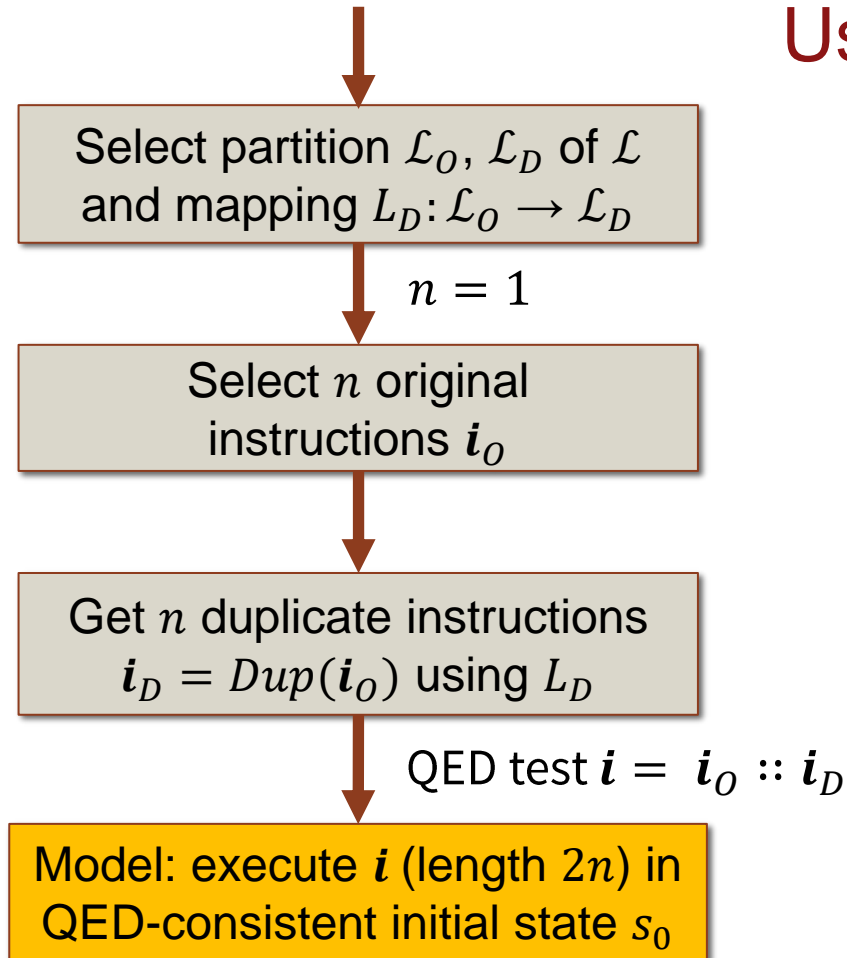
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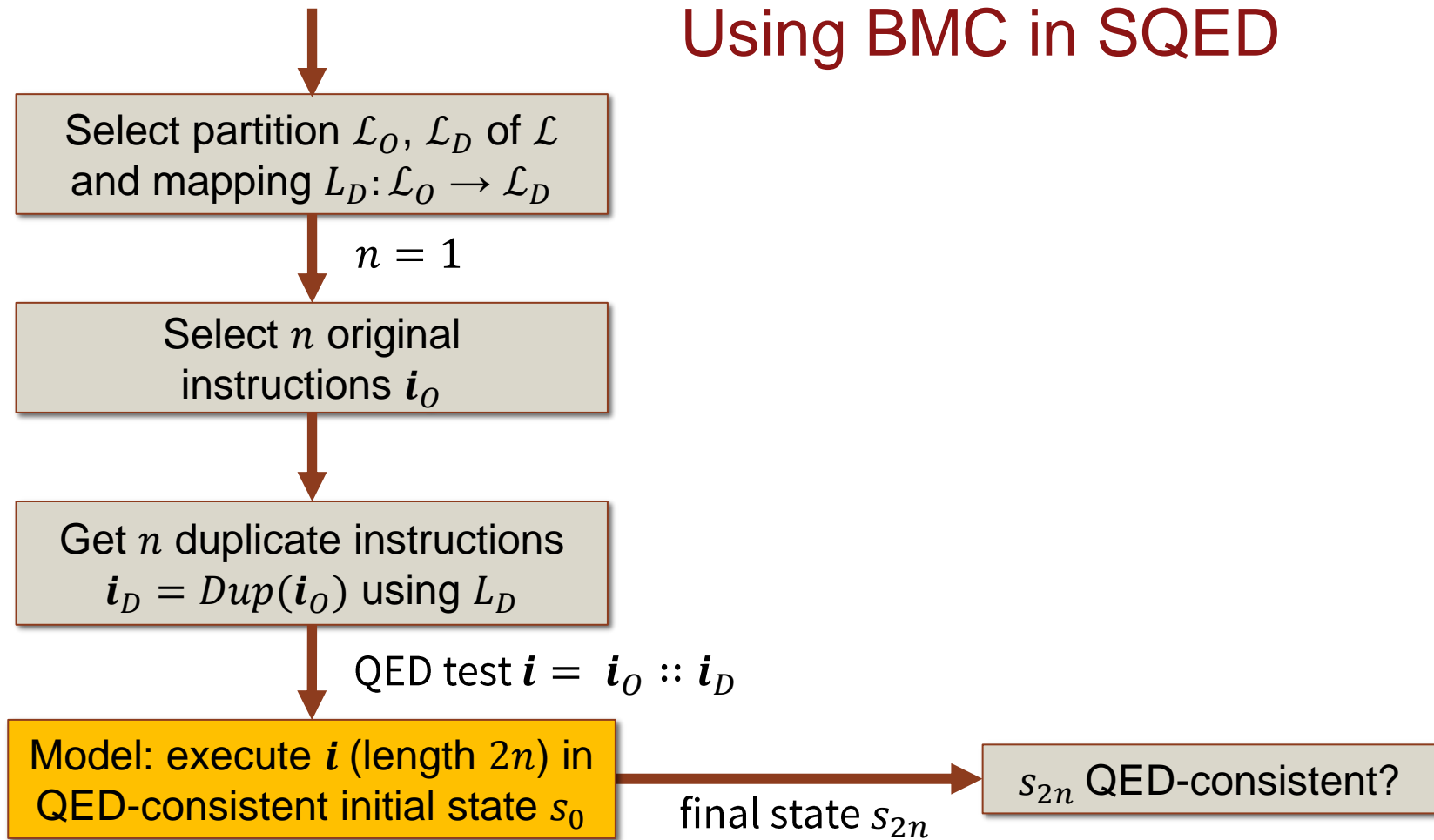
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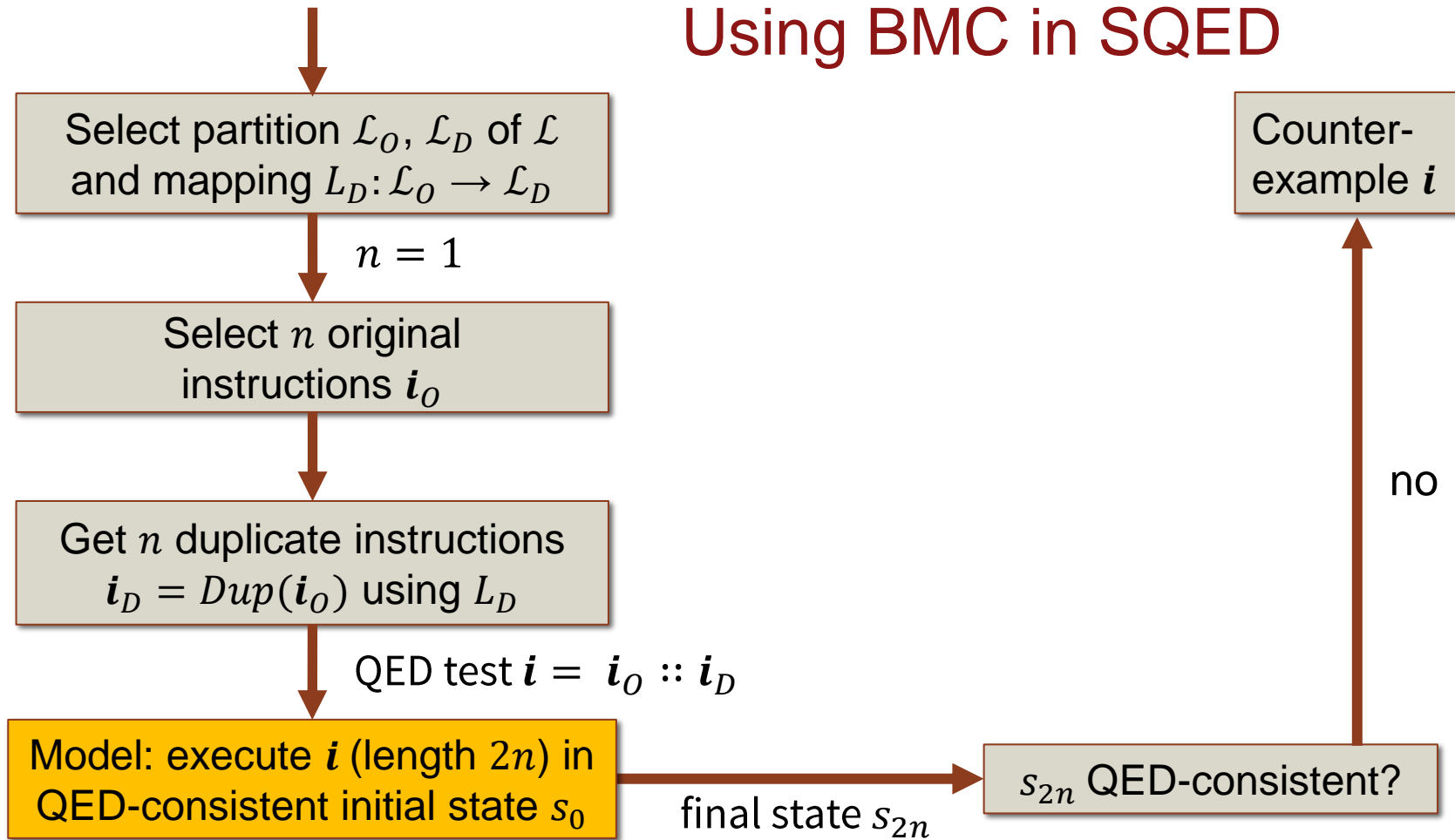
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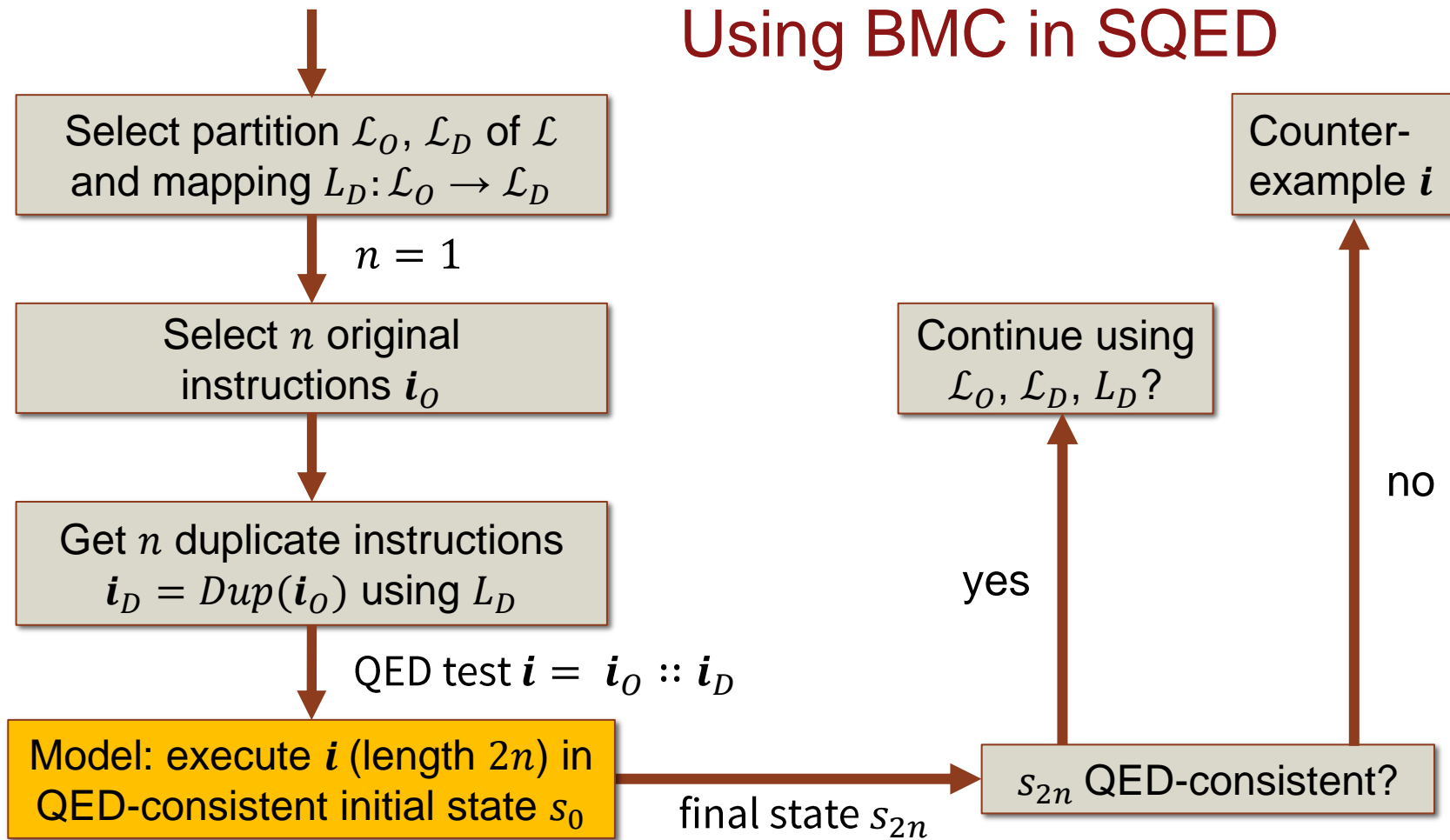
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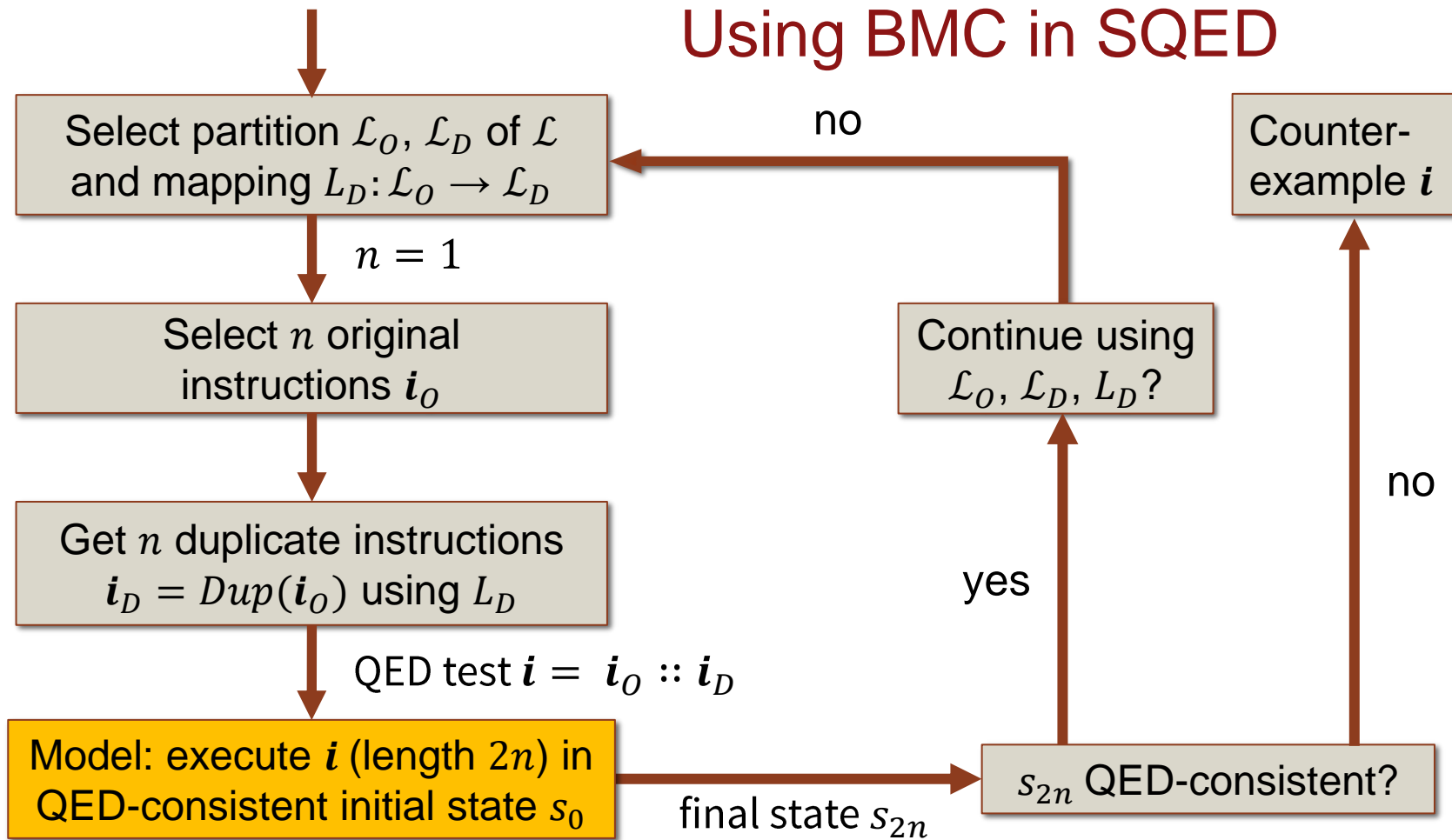
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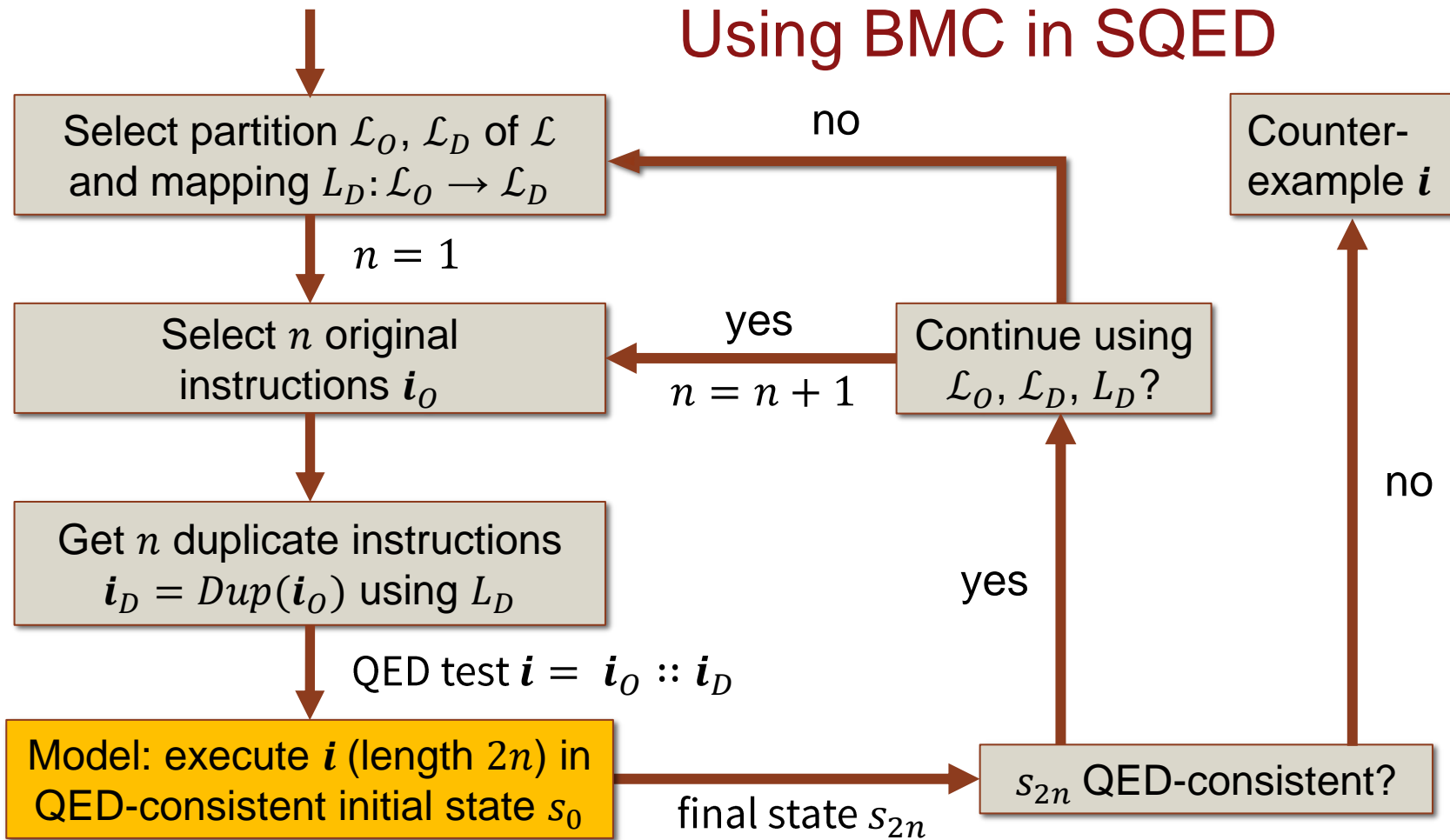
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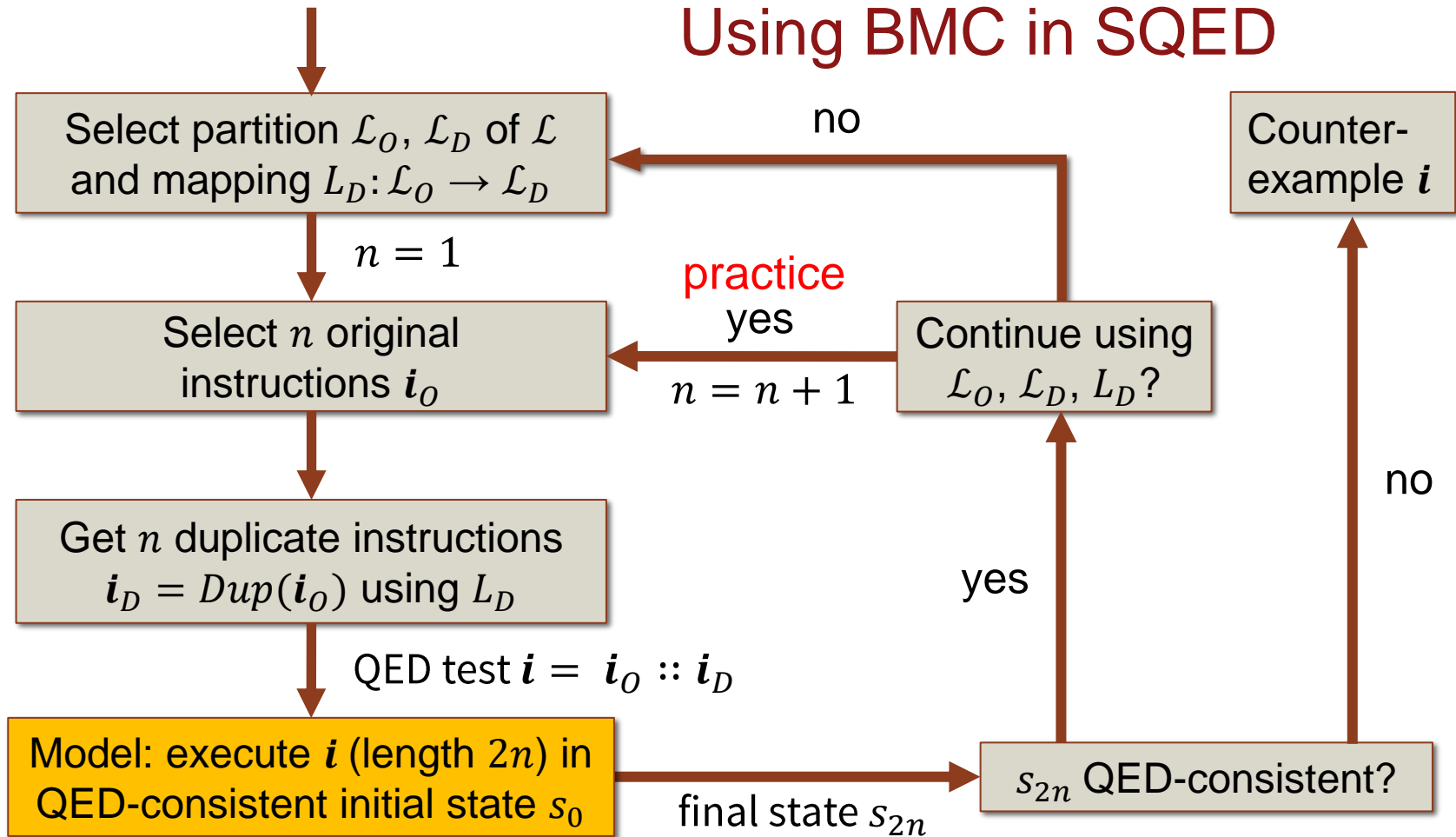
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Using BMC in SQED



Abstract Specification Relation

$$\begin{aligned} & \forall s, s' \in S, i \in I. \text{Spec}(s, i, s') \leftrightarrow \forall l \in \mathcal{L}. \\ & (l \neq \text{LocOut}(i) \rightarrow s(l) = s'(l)) \wedge \\ & (l = \text{LocOut}(i) \rightarrow s'(l) = \text{SpecOut}(i, s(\text{LocIn}(i)))) \end{aligned}$$

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- Transition $T(s, i) = s'$ according to $\text{Spec} \subseteq S \times I \times S$ iff:
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 - Output specification: $\text{SpecOut}: I \times \mathcal{V}^2 \rightarrow \mathcal{V}$.

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- Abstract spec needed **only for theory**, not practice.

Bugs and Processor Correctness

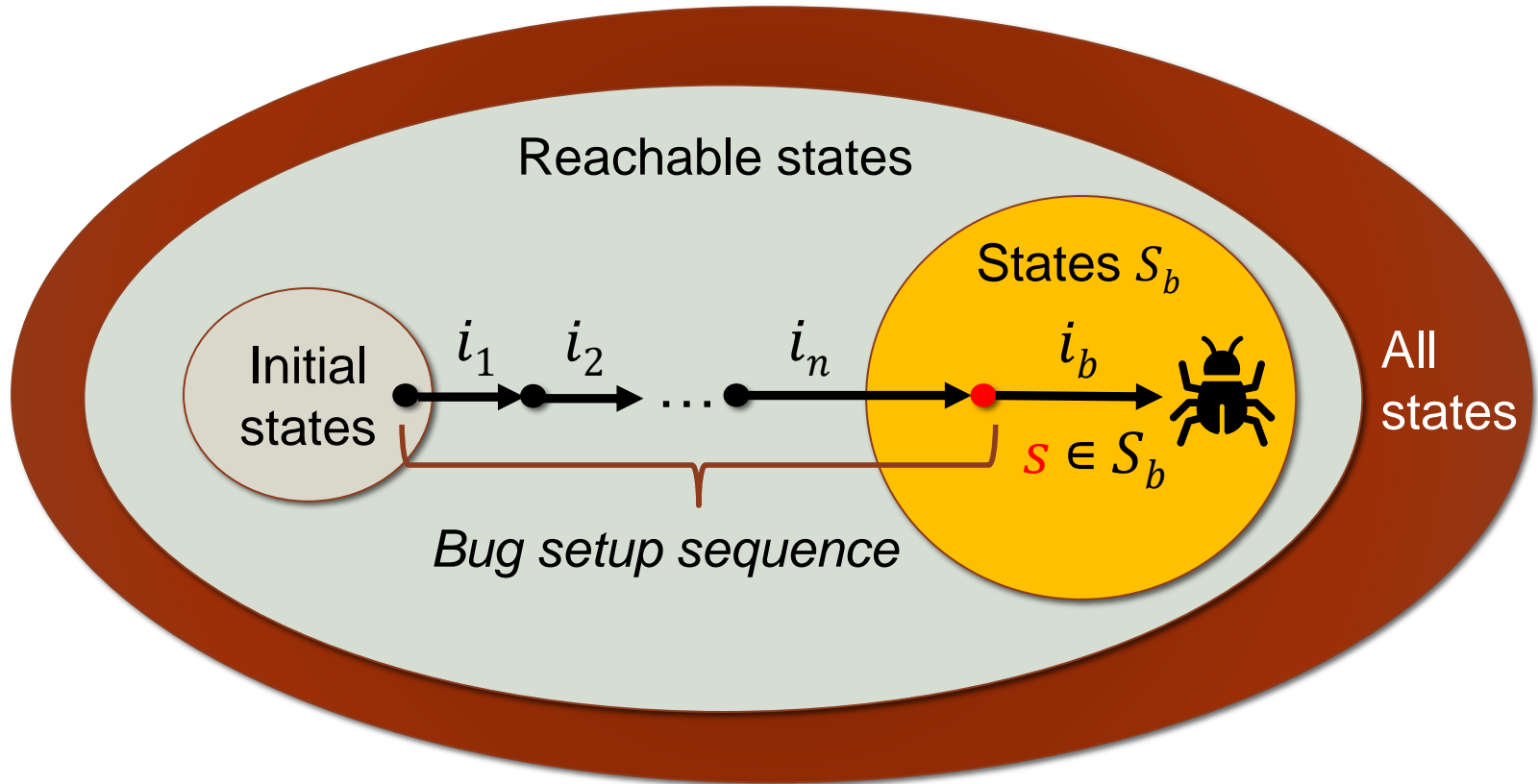
Processor P is **correct** wrt. Spec:

- $\forall s \in S, i \in I. reach(s) \rightarrow Spec(s, i, T(s, i)).$
- All instructions execute correctly in all **reachable** states.

Bug:

- Instruction i_b and set $S_b \subseteq S$ of **bug-triggering states**.
- $S_b = \{s \in S \mid reach(s) \wedge \sim Spec(s, i_b, T(s, i_b))\}$

Bugs and Processor Correctness



Single-Instruction Bugs and Correctness

Processor P is **single-instruction (SI) correct** wrt. Spec:

- $\forall s \in \mathit{Init}, i \in I. \text{Spec}(s, i, T(s, i)).$
- All instructions execute correctly in all **initial states *Init***.

Single-Instruction Bugs and Correctness

Processor P is single-instruction (SI) correct wrt. $Spec$:

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Single-instruction (SI) bug:

- $\exists s \in Init, i \in I. \sim Spec(s, i, T(s, i)).$
- No setup sequence, well-studied approaches to checking.

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Single-instruction (SI) bug:

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- No setup sequence, well-studied approaches to checking.



Assumption: P is SI-correct.

Soundness of SQED

QED test $\mathbf{i} = \mathbf{i}_O :: \mathbf{i}_D$ fails iff

- QED-consistent initial state $s_0 \in \text{Init}$,
- QED-inconsistent final state $s = T(s_0, \mathbf{i})$.

Soundness of SQED

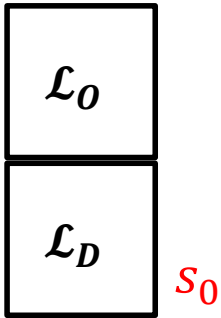
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Theorem: *if there exists a failing QED test for P , then P has a bug wrt. to some abstract Spec .*

Towards Completeness: Bug-Specific QED Test

$QEDcons(s_0)$



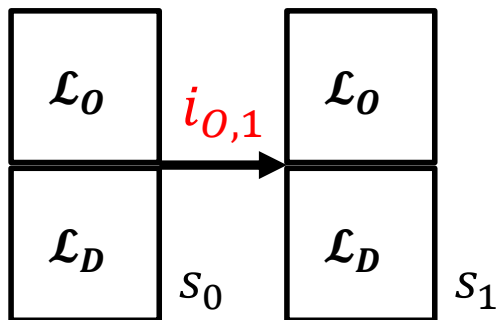
Initial state

QED test $\mathbf{i} = (i_{O,1}, \dots, i_{O,n}) :: (i_{D,1}, \dots, i_{D,n})$ for some L_D .

- Flexibility in choosing L_D .
- QED-consistent **initial state** s_0 .

Towards Completeness: Bug-Specific QED Test

$QEDcons(s_0)$



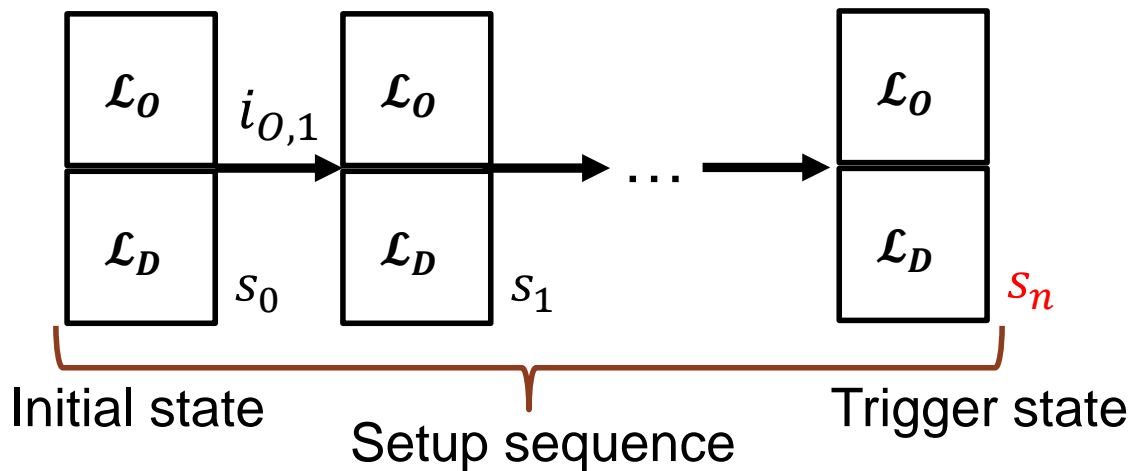
Initial state

QED test $\mathbf{i} = (i_{O,1}, \dots, i_{O,n}) :: (i_{D,1}, \dots, i_{D,n})$ for some L_D .

- QED-consistent initial state s_0 .
- Let $i_b = Dup(i_{O,1})$: $i_{O,1}$ meets $Spec$ due to SI-correctness.

Towards Completeness: Bug-Specific QED Test

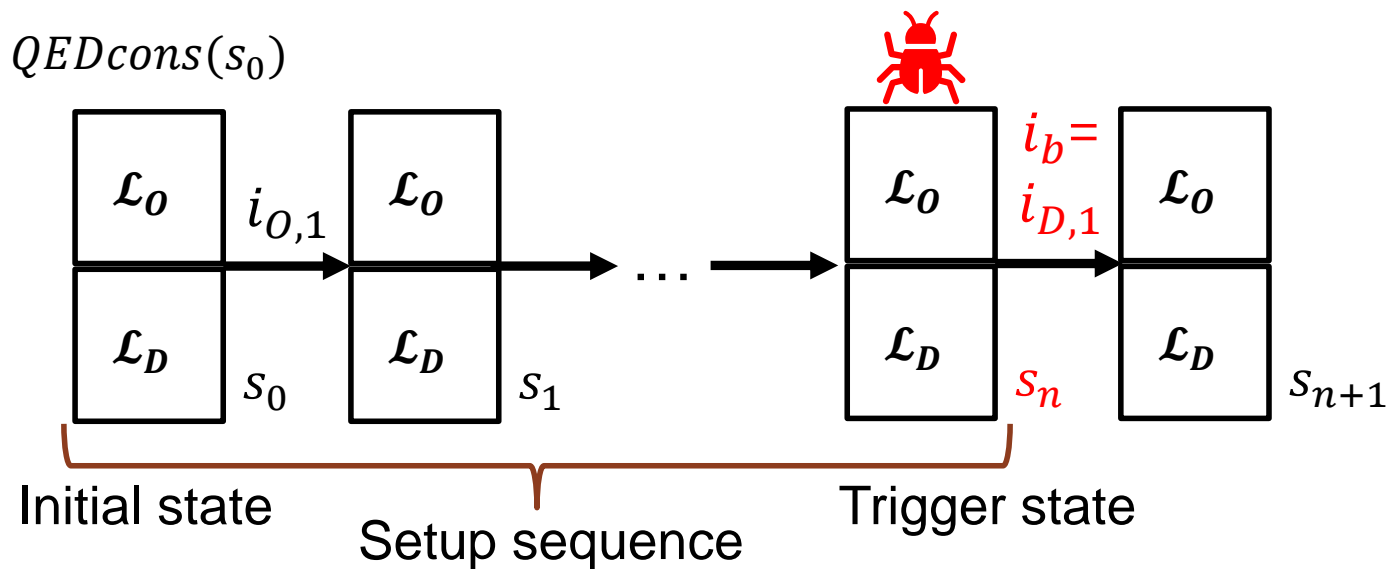
$QEDcons(s_0)$



QED test $\mathbf{i} = (i_{O,1}, \dots, i_{O,n}) :: (i_{D,1}, \dots, i_{D,n})$ for some L_D .

- Setup sequence $i_{O,1}, \dots, i_{O,n}$ to reach triggering state $s_n \in S_b$.

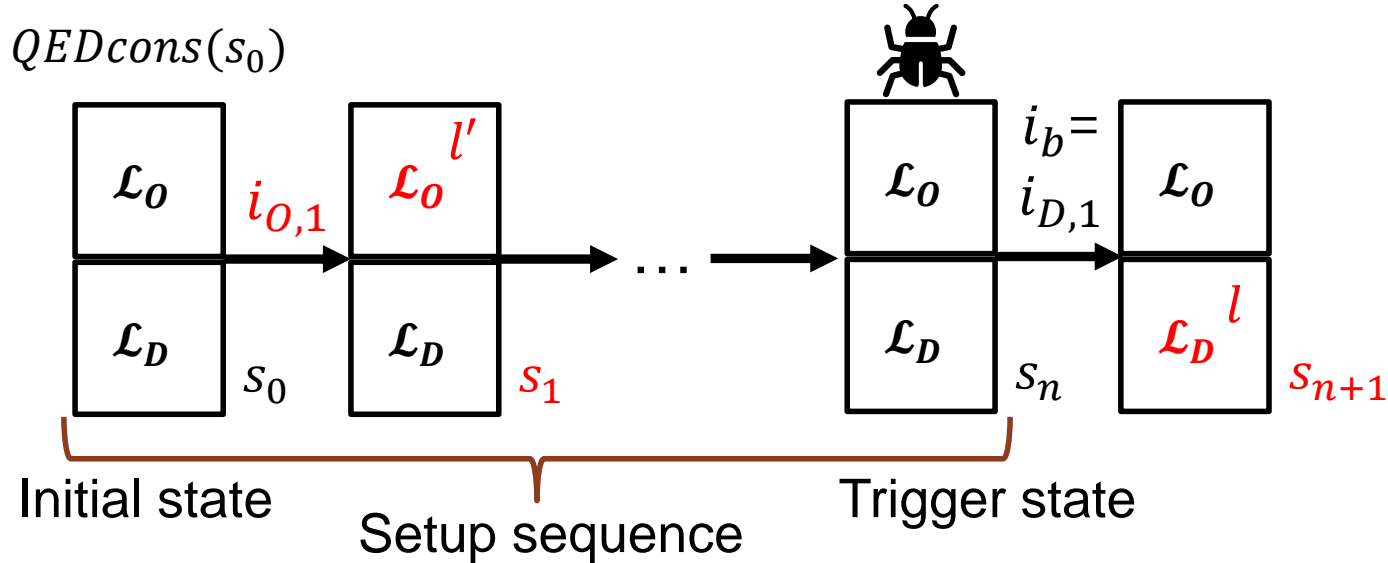
Towards Completeness: Bug-Specific QED Test



QED test $\mathbf{i} = (i_{O,1}, \dots, i_{O,n}) :: (i_{D,1}, \dots, i_{D,n})$ for some L_D .

- Setup sequence $i_{O,1}, \dots, i_{O,n}$ to reach triggering state $s_n \in S_b$.
- Bug instruction $i_b = Dup(i_{O,1})$ fails in s_n .

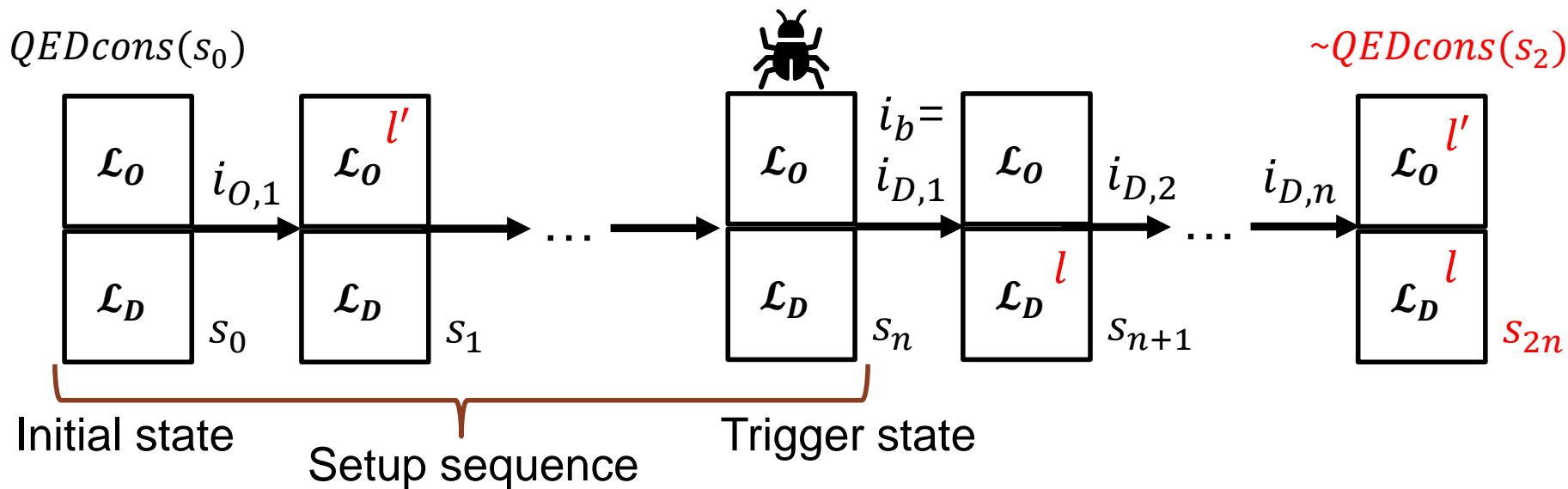
Towards Completeness: Bug-Specific QED Test



QED test $\mathbf{i} = (i_{O,1}, \dots, i_{O,n}) :: (i_{D,1}, \dots, i_{D,n})$ for some L_D .

- E.g. wrong value at output location l of i_b in s_{n+1} .
- Correct value at original output location l' of $i_{O,1}$ in s_1 .

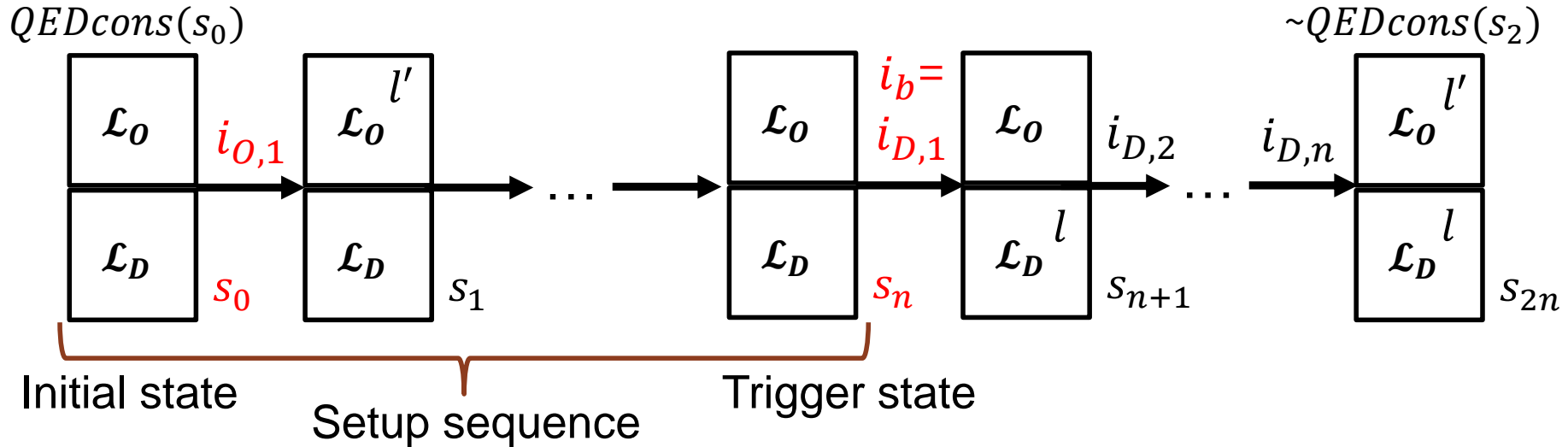
Towards Completeness: Bug-Specific QED Test



QED test $\mathbf{i} = (i_{O,1}, \dots, i_{O,n}) :: (i_{D,1}, \dots, i_{D,n})$ for some L_D .

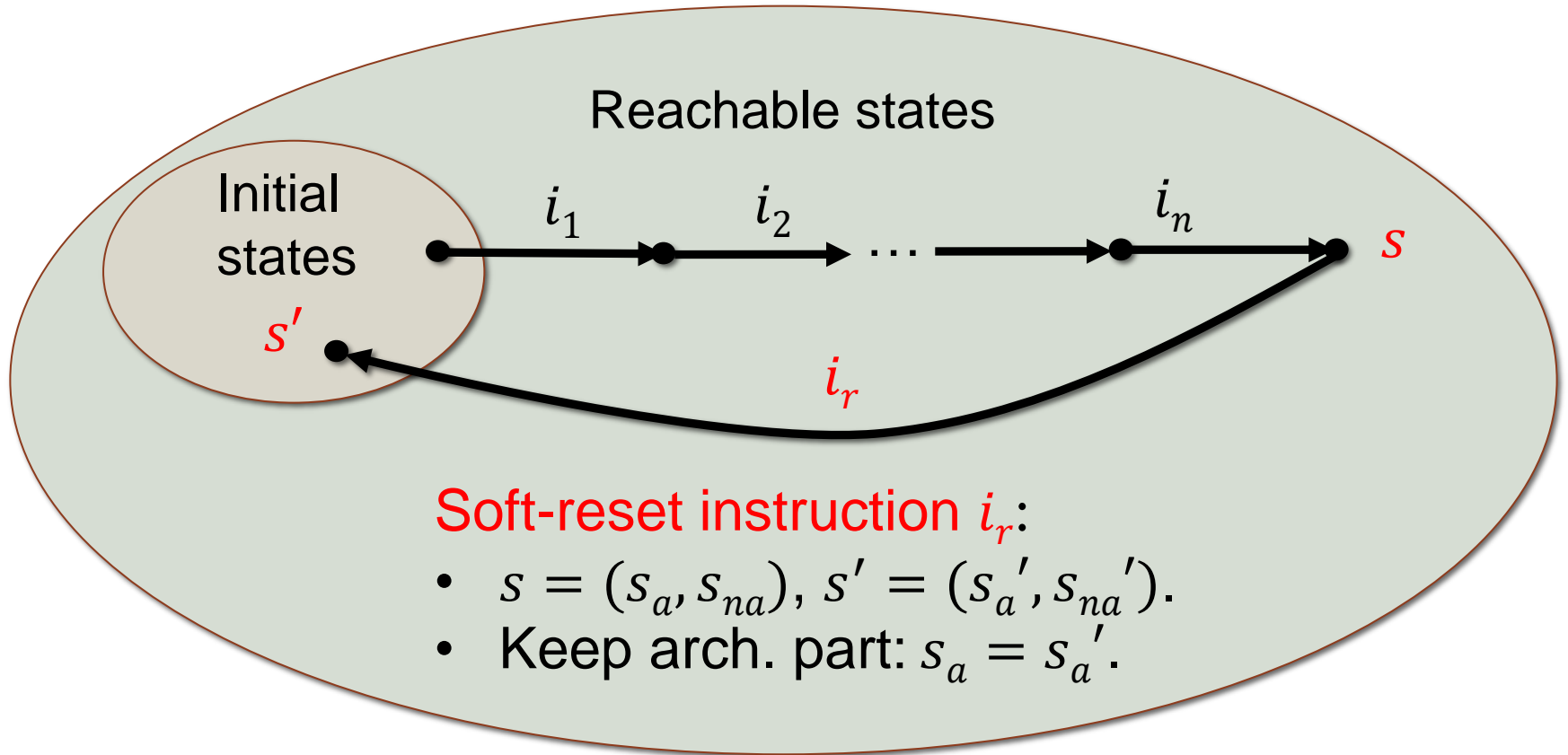
- Mismatching values at locations l and l' in s_{2n} .
- Final state s_{2n} **QED-inconsistent**.

Conditional Completeness

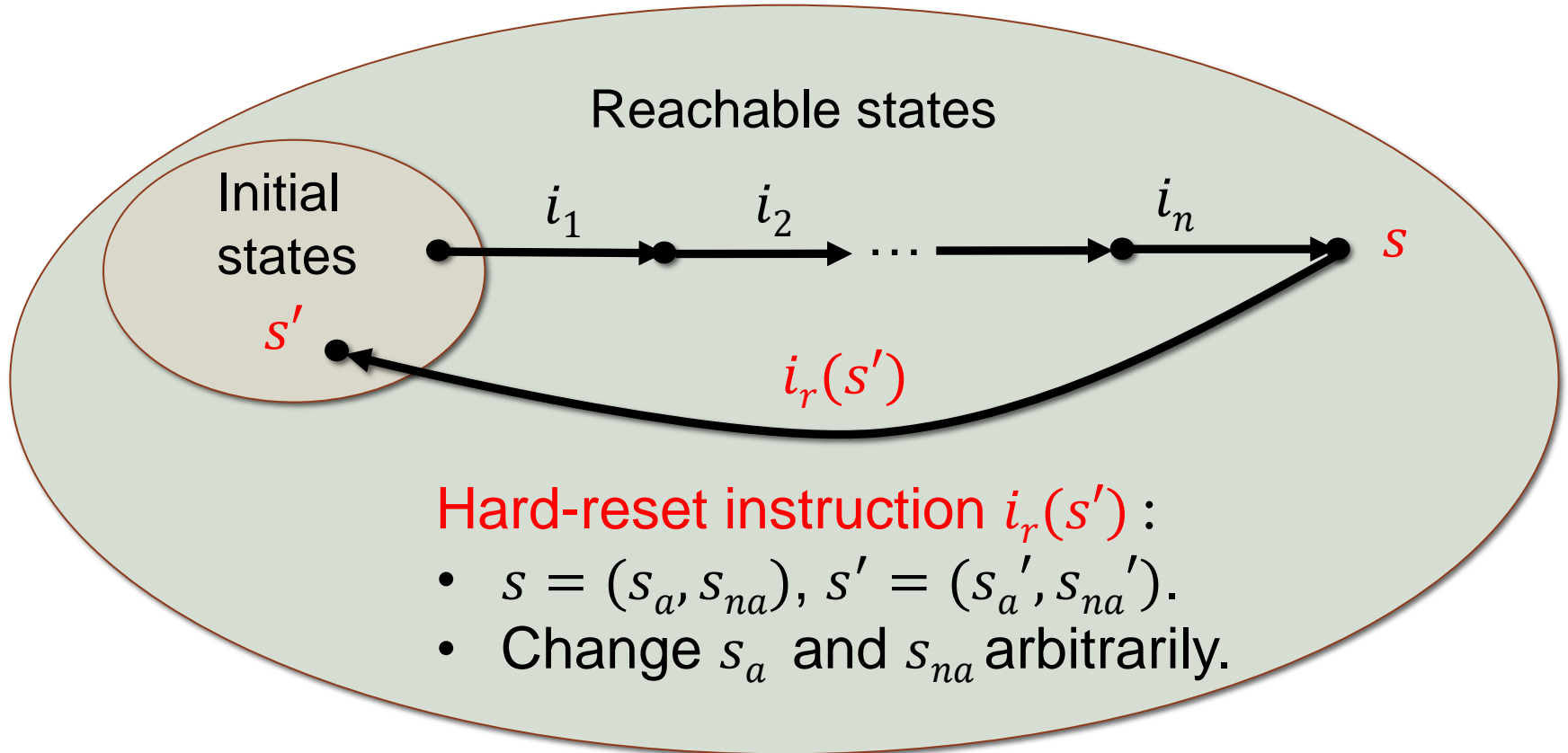


Theorem: *if a bug-specific QED test i exists, then i fails.*

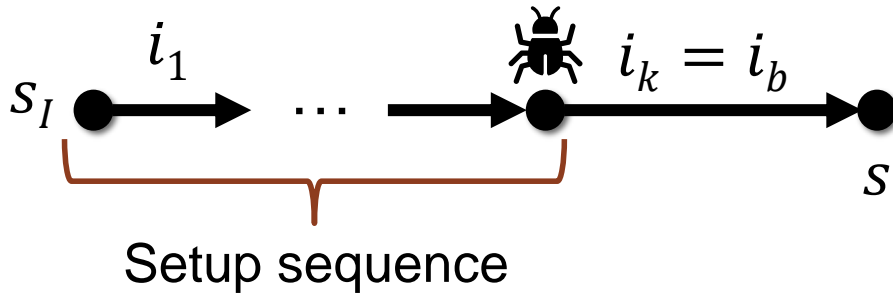
Extensions: Reset Instructions



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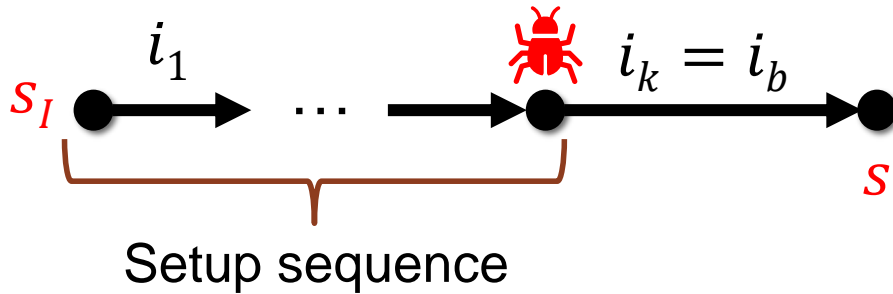


Extensions: QED Test with Reset



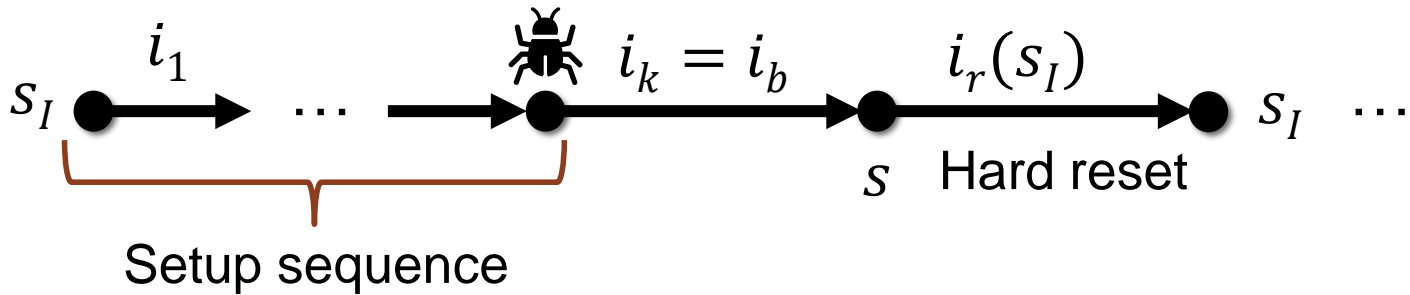
- Bug set up and triggered by $i_1, \dots, i_k = i_b$.
- **No duplication**: check states after $i_k = i_b$ with(out) reset.

Extensions: QED Test with Reset



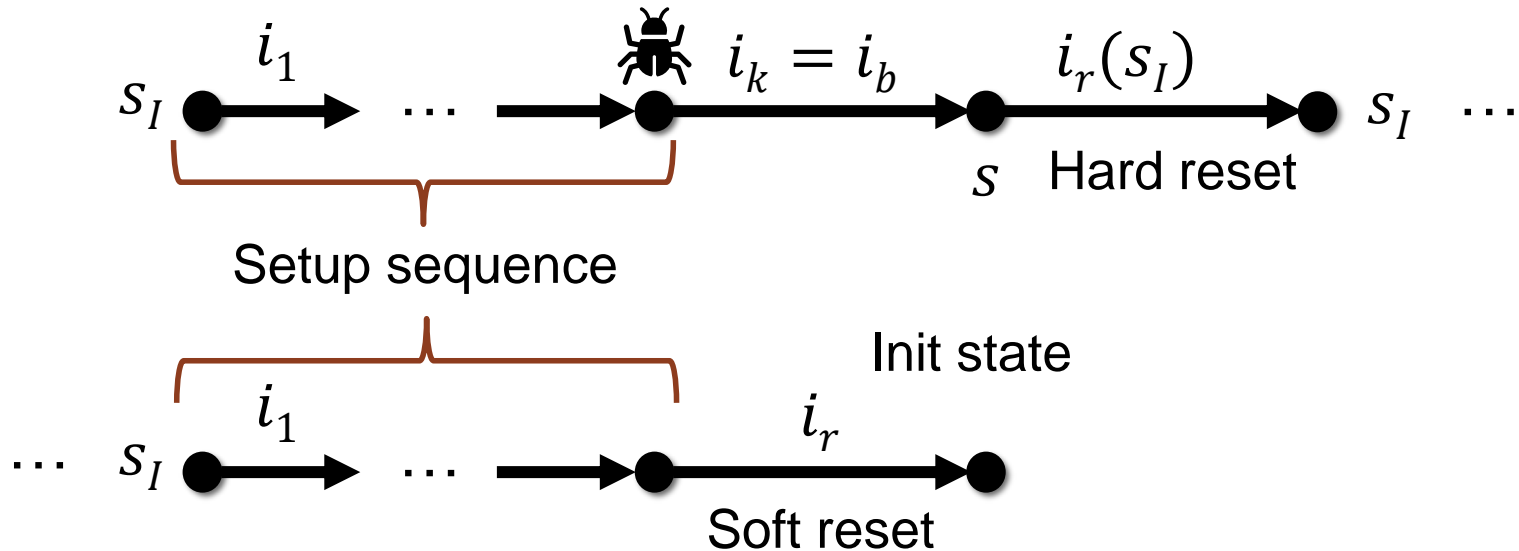
- Bug set up and triggered by $i_1, \dots, i_k = i_b$.
- Execute $i_1, \dots, i_k = i_b$ from $s_I \in \text{Init}$: wrong value in state s .

Extensions: QED Test with Reset



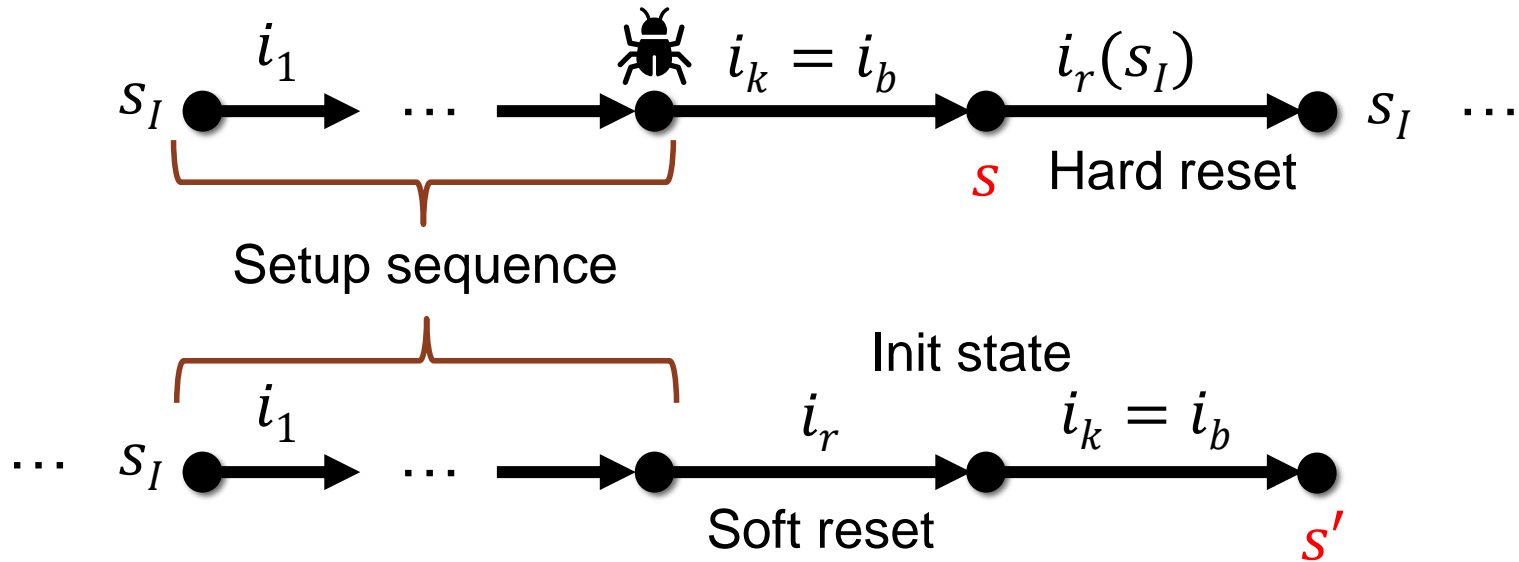
- Execute hard reset in state s , get back to s_I .
- Idea: execute $i_1, \dots, i_k = i_b$ again with soft reset before i_b .

Extensions: QED Test with Reset



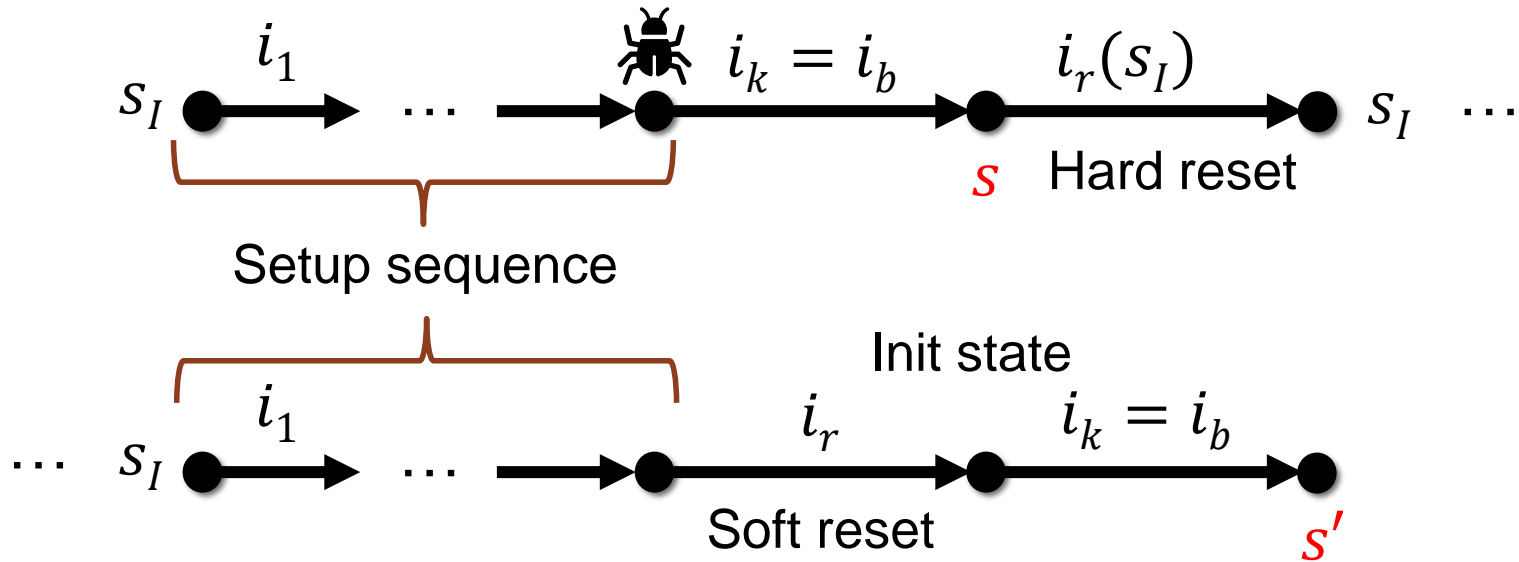
- Execute soft reset in bug-triggering state before $i_k = i_b$.
- Make use of SI correctness.

Extensions: QED Test with Reset



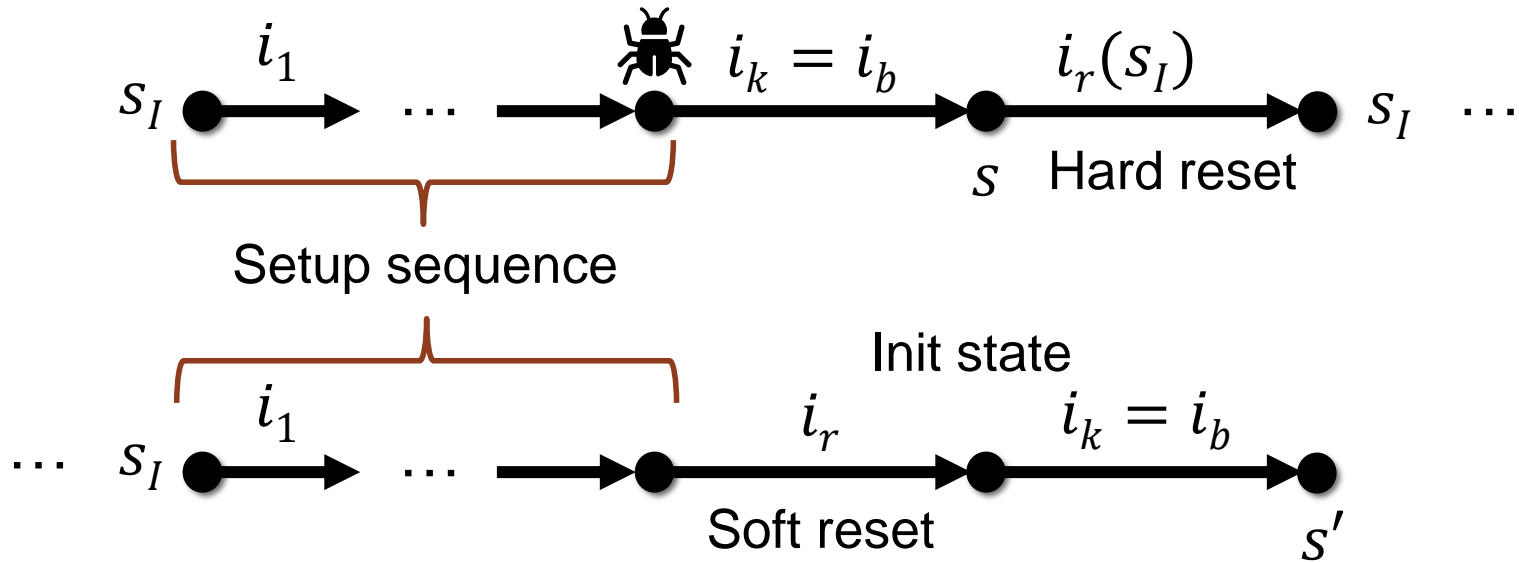
- Bug instruction $i_k = i_b$ executes correctly.
- Compare s and final state s' .

Extensions: QED Test with Reset



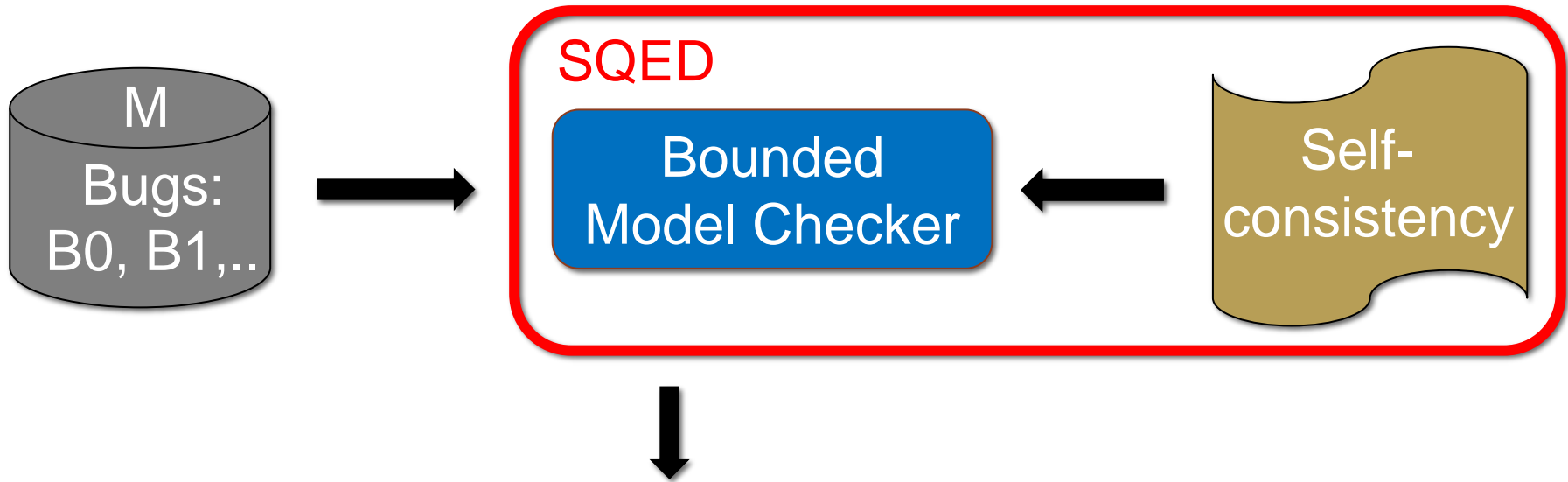
- QED test with reset fails iff $s(l) \neq s'(l)$ for a location l .

Extensions: QED Test with Reset



Theorem (full completeness): *if P is SI correct and has no failing QED test with reset, then P is correct.*

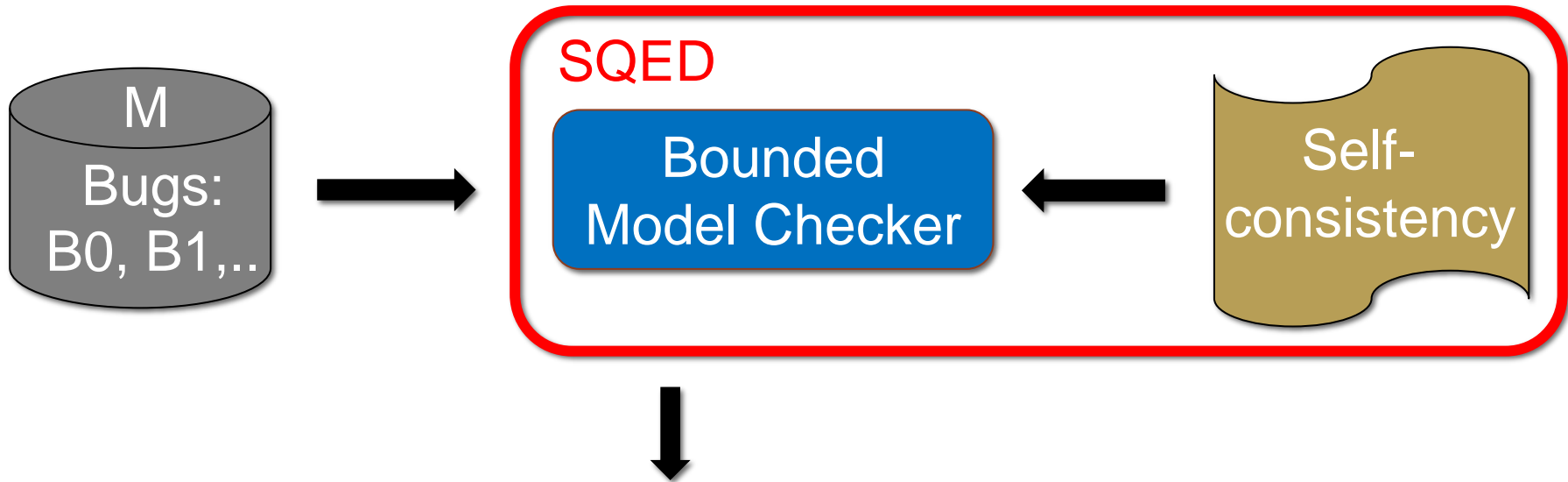
Summary: SQED Soundness and Completeness



- If M not self-consistent then $B \in M$.
- Self-consistency covers bug B .

No spurious cex

Summary: SQED Soundness and Completeness



- If $B \in M$ then M not self-consistent.
- Self-consistency covers bug B .

Conditional/full
Completeness

Future Work

Leveraging QED test extensions:

- Soft/hard reset not yet applied in practice.
- Design-for-verification approach.

Formal model refinements:

- Instruction pipelines, multiprocessor systems.
- Deadlock detection.
- Symbolic starting states.

Thank you for watching this video!